Classification-Aware Hidden-Web Text Database Selection

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Many valuable text databases on the web have noncrawable contents that are “hidden” behind search interfaces. Metasearchers are helpful tools for searching over multiple such “hidden-web” text databases at once through a unified query interface. An important step in the metasearching process is database selection, or determining which databases are the most relevant for a given user query. The state-of-the-art database selection techniques rely on statistical summaries of the database contents, generally including the database vocabulary and associated word frequencies. Unfortunately, hidden-web text databases typically do not export such summaries, so previous research has developed algorithms for constructing approximate content summaries from document samples extracted from the databases via querying. We present a novel “focused-probing” sampling algorithm that detects the topics covered in a database and adaptively extracts documents that are representative of the topic coverage of the database. Our algorithm is the first to construct content summaries that include the frequencies of the words in the database. Unfortunately, Zipf’s law practically guarantees that for any relatively large database, content summaries built from moderately sized document samples will fail to cover many low-frequency words; in turn, incomplete content summaries might negatively affect the database selection process, especially for short queries with infrequent words. To enhance the sparse document samples and improve the database selection decisions, we exploit the fact that topically similar databases tend to have similar vocabularies, so samples extracted from databases with a similar topical focus can complement each other. We have developed two database selection algorithms that exploit this observation. The first algorithm proceeds hierarchically and selects the best categories for a query, and then sends the query to the appropriate databases in the chosen categories. The second algorithm uses...
“shrinkage,” a statistical technique for improving parameter estimation in the face of sparse data, to enhance the database content summaries with category-specific words. We describe how to modify existing database selection algorithms to adaptively decide (at runtime) whether shrinkage is beneficial for a query. A thorough evaluation over a variety of databases, including 315 real web databases as well as TREC data, suggests that the proposed sampling methods generate high-quality content summaries and that the database selection algorithms produce significantly more relevant database selection decisions and overall search results than existing algorithms.

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1. INTRODUCTION

The World-Wide Web continues to grow rapidly, which makes exploiting all useful information that is available a standing challenge. Although general web search engines crawl and index a large amount of information, typically they ignore valuable data in text databases that is “hidden” behind search interfaces and whose contents are not directly available for crawling through hyperlinks.

Example 1.1. Consider the U.S. Patent and Trademark (USPTO) database, which contains the full text of all patents awarded in the US since 1976. If we query the USPTO for patents with the keywords “wireless” and “network”, USPTO returns 62,231 matches as of June 6th, 2007, corresponding to distinct patents that contain these keywords. In contrast, a query on Google's main index that finds those pages in the USPTO database with the keywords “wireless” and “network” returns two matches as of June 6th, 2007. This illustrates that valuable content available through the USPTO database is ignored by this search engine.

One way to provide one-stop access to the information in text databases is through metasearchers, which can be used to query multiple databases

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1The full text of the patents is stored at the USPTO site.
2The query interface is available at http://patft.uspto.gov/netahtml/PTO/search-adv.htm
3The query is [wireless AND network].
4The query is [wireless network site:patft.uspto.gov].
5Google has a dedicated patent-search service that specifically hosts and enables searches over the USPTO contents; see http://www.google.com/patents

A metasearcher performs three main tasks. After receiving a query, it finds the best databases to evaluate it (database selection), translates the query in a suitable form for each database (query translation), and finally retrieves and merges the results from different databases (result merging) and returns them to the user. The database selection component of a metasearcher is of crucial importance in terms of both query processing efficiency and effectiveness.

Database selection algorithms are often based on statistics that characterize each database's contents [Yuwono and Lee 1997; Xu and Callan 1998; Meng et al. 1998; Gravano et al. 1999]. These statistics, to which we will refer as content summaries, usually include the document frequencies of the words that appear in the database, plus perhaps other simple statistics. These summaries provide sufficient information to the database selection component of a metasearcher to decide which databases are the most promising to evaluate a given query.

Constructing the content summary of a text database is a simple task if the full contents of the database are available (e.g., via crawling). However, this task is challenging for so-called hidden-web text databases, whose contents are only available via querying. In this case, a metasearcher could rely on the databases to supply the summaries (e.g., by following a protocol like STARTS [Gravano et al. 1997], or possibly by using semantic web [Berners-Lee et al. 2001] tags in the future). Unfortunately, many web-accessible text databases are completely autonomous and do not report any detailed metadata about their contents to facilitate metasearching. To handle such databases, a metasearcher could rely on manually generated descriptions of the database contents. Such an approach would not scale to the thousands of text databases available on the web [Bergman 2001], and would likely not produce the good-quality, fine-grained content summaries required by database selection algorithms.

In this article, we first present a technique to automate the extraction of high-quality content summaries from hidden-web text databases. Our technique constructs these summaries from a biased sample of the documents in a database, extracted by adaptively probing the database using the topically focused queries sent to the database during a topic classification step. Our algorithm selects what queries to issue based in part on the results of earlier queries, thus focusing on those topics that are most representative of the database in question. Our technique resembles biased sampling over numeric databases, which focuses the sampling effort on the “densest” areas. We show that this principle is also beneficial for the text-database world. Interestingly, our technique moves beyond the document sample and attempts to include in the content summary of a database accurate estimates of the actual document frequency of words in the database. For this, our technique exploits well-studied statistical properties of text collections.

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6Other database selection algorithms (e.g., Si and Callan [2005, 2004a, 2003], Hawking and Thomas [2005], Shokouhi [2007]) also use document samples from the databases to make selection decisions.
Unfortunately, all efficient techniques for building content summaries via document sampling suffer from a sparse-data problem: Many words in any text database tend to occur in relatively few documents, so any document sample of reasonably small size will necessarily miss many words that occur in the associated database only a small number of times. To alleviate this sparse-data problem, we exploit the observation (which we validate experimentally) that incomplete content summaries of topically related databases can be used to complement each other. Based on this observation, we explore two alternative algorithms that make database selection more resilient to incomplete content summaries. Our first algorithm selects databases hierarchically, based on their categorization. The algorithm first chooses the categories to explore for a query and then picks the best databases in the most appropriate categories. Our second algorithm is a “flat” selection strategy that exploits the database categorization implicitly by using “shrinkage,” a statistical technique for improving parameter estimation in the face of sparse data. Our shrinkage-based algorithm enhances the database content summaries with category-specific words. As we will see, shrinkage-enhanced summaries often characterize the database contents better than their “unshrunk” counterparts do. Then, during database selection, our algorithm decides in an adaptive and query-specific way whether an application of shrinkage would be beneficial.

We evaluate the performance of our content summary construction algorithms using a variety of databases, including 315 real web databases. We also evaluate our database selection strategies with extensive experiments that involve text databases and queries from the TREC testbed, together with relevance judgments associated with queries and database documents. We compare our methods with a variety of database selection algorithms. As we will see, our techniques result in a significant improvement in database selection quality over existing techniques, achieved efficiently just by exploiting the database classification information and without increasing the document-sample size.

In brief, the main contributions presented in this article are as follows:

— a technique to sample text databases that results in higher-quality database content summaries than those produced by state-of-the-art alternatives;
— a technique to estimate the absolute document frequencies of the words in content summaries;
— a technique to improve the quality of sample-based content summaries using shrinkage;
— a hierarchical database selection algorithm that works over a topical classification scheme;
— an adaptive database selection algorithm that decides in an adaptive and query-specific way whether to use the shrinkage-based content summaries; and
— a thorough, extensive experimental evaluation of the presented algorithms using a variety of datasets, including TREC data and 315 real web databases.

The rest of the article is organized as follows. Section 2 gives the necessary background. Section 3 outlines our new technique for producing content summaries.
Table I. A Fragment of the Content Summaries of Two Databases

<table>
<thead>
<tr>
<th></th>
<th>CANCERLIT</th>
<th></th>
<th>CNN Money</th>
</tr>
</thead>
<tbody>
<tr>
<td>Word</td>
<td></td>
<td>df</td>
<td>Word</td>
</tr>
<tr>
<td>breast</td>
<td>3,801,351</td>
<td>181,102</td>
<td>breast</td>
</tr>
<tr>
<td>cancer</td>
<td>1,893,838</td>
<td></td>
<td>cancer</td>
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<tr>
<td>...</td>
<td>...</td>
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</tr>
</tbody>
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summaries of text databases and presents our frequency estimation algorithm. Section 4 describes our hierarchical and shrinkage-based database selection algorithms, which build on our observation that topically similar databases have similar content summaries. Section 5 describes the settings for the experimental evaluation of Sections 6 and 7. Finally, Section 8 describes related work and Section 9 concludes the article.

2. BACKGROUND

In this section, we provide the required background and describe related efforts. Section 2.1 briefly summarizes how existing database selection algorithms work, stressing their reliance on database “content summaries.” Then, Section 2.2 describes the use of “uniform” query probing for extraction of content summaries from text databases, and identifies the limitations of this technique. Finally, Section 2.3 discusses how focused query probing has been used in the past for the classification of text databases.

2.1 Database Selection Algorithms

Database selection is an important task in the metasearching process, since it has a critical impact on the efficiency and effectiveness of query processing over multiple text databases. We now briefly outline how typical database selection algorithms work and how they depend on database content summaries to make decisions.

A database selection algorithm attempts to find the best text databases to evaluate a given query, based on information about the database contents. Usually, this information includes the number of different documents that contain each word, which we refer to as the document frequency of the word, plus perhaps some other simple related statistics [Gravano et al. 1997; Meng et al. 1998; Xu and Callan 1998], such as the number of documents stored in the database.

Definition 2.1. The content summary $S(D)$ of a database $D$ consists of:

— the actual number of documents in $D$, $|D|$, and
— for each word $w$, the number $df(w)$ of documents in $D$ that include $w$.

For notational convenience, we also use $p(w|D) = \frac{df(w)}{|D|}$ to denote the fraction of $D$ documents that include $w$.

Table I shows a small fraction of what the content summaries for two real text databases might look like. For example, the content summary for the CNN
Money database, a database with articles about finance, indicates that 255 out of the 13,313 documents in this database contain the word “cancer,” while there are 1,893,838 documents with the word “cancer” in CANCERLIT, a database with research articles about cancer. Given these summaries, a database selection algorithm estimates the relevance of each database for a given query (e.g., in terms of the number of matches that each database is expected to produce for the query).

Example 2.2. bGLOSS [Gravano et al. 1999] is a simple database selection algorithm that assumes query words to be independently distributed over database documents to estimate the number of documents that match a given query. So, bGLOSS estimates that query [breast cancer] will match $|D| \cdot \frac{df(breast)}{|D|} \cdot \frac{df(cancer)}{|D|} \approx 90,225$ documents in database CANCERLIT, where $|D|$ is the number of documents in the CANCERLIT database and $df(w)$ is the number of documents that contain the word $w$. Similarly, bGLOSS estimates that roughly only one document will match the given query in the other database, CNN Money, of Table I.

bGLOSS is a simple example from a large family of database selection algorithms that rely on content summaries such as those in Table I. Furthermore, database selection algorithms expect content summaries to be accurate and up-to-date. The most desirable scenario is when each database exports its content summary directly and reliably (e.g., via a protocol such as STARTS [Gravano et al. 1997]). Unfortunately, no protocol is widely adopted for web-accessible databases, and there is little hope that such a protocol will emerge soon. Hence, we need other solutions to automate the construction of content summaries from databases that cannot or are not willing to export such information. We review one such approach next.

2.2 Uniform Probing for Content Summary Construction

As discussed before, we cannot extract perfect content summaries for hidden-web text databases whose contents are not crawlable. When we do not have access to the complete content summary $S(D)$ of a database $D$, we can only hope to generate a good approximation to use for database selection purposes.

Definition 2.3. The approximate content summary $\hat{S}(D)$ of a database $D$ consists of:

— an estimate $\hat{|D|}$ of the number of documents in $D$, and
— for each word $w$, an estimate $\hat{df}(w)$ of $df(w)$.

Using the values $\hat{|D|}$ and $\hat{df}(w)$, we can define an approximation $\hat{p}(w|D)$ of $p(w|D)$ as $\hat{p}(w|D) = \frac{\hat{df}(w)}{\hat{|D|}}$.

Callan et al. [1999] and Callan and Connell [2001] presented pioneering work on automatic extraction of approximate content summaries from “uncooperative” text databases that do not export such metadata. Their algorithm extracts a document sample via querying from a given database $D$, and approximates
df(w) using the frequency of each observed word w in the sample, sf(w) (i.e., df(w) = sf(w)). In detail, the algorithm proceeds as follows.

**Algorithm.**

1. Start with an empty content summary where sf(w) = 0 for each word w, and a general (i.e., not specific to D), comprehensive word dictionary.
2. Pick a word (see the next paragraph) and send it as a query to database D.
3. Retrieve the top-k documents returned for the query.
4. If the number of retrieved documents exceeds a prespecified threshold, stop. Otherwise continue the sampling process by returning to step 2.

Callan et al. suggested using k = 4 for step 3 and that 300 documents are sufficient (step 4) to create a representative content summary of a database. Also they describe two main versions of this algorithm that differ in how step 2 is executed. The algorithm QueryBasedSampling-OtherResource (QBS-Ord for short) picks a random word from the dictionary for step 2. In contrast, the algorithm QueryBasedSampling-LearnedResource (QBS-Lrd for short) selects the next query from among the words that have been already discovered during sampling. QBS-Ord constructs better profiles, but is more expensive than QBS-Lrd [Callan and Connell 2001]. Other variations of this algorithm perform worse than QBS-Ord and QBS-Lrd, or have only marginal improvement in effectiveness at the expense of probing cost.

Unfortunately, both QBS-Lrd and QBS-Ord have a few shortcomings. Since these algorithms set df(w) = sf(w), the approximate frequencies df(w) range between zero and the number of retrieved documents in the sample. In other words, the actual document frequency df(w) for each word w in the database is not revealed by this process. Hence, two databases with the same focus (e.g., two medical databases) but differing significantly in size might be assigned similar content summaries. Also, QBS-Ord tends to produce inefficient executions in which it repeatedly issues queries to databases that produce no matches. According to Zipf’s law [Zipf 1949], most of the words in a collection occur very few times. Hence, a word that is randomly picked from a dictionary (which hopefully contains a superset of the words in the database), is not likely to occur in any document of an arbitrary database. Similarly, for QBS-Lrd, the queries are derived from the already acquired vocabulary, and many of these words appear only in one or two documents, so a large fraction of the QBS-Lrd queries return only documents that have been retrieved before. These queries increase the number of queries sent by QBS-Lrd, but do not retrieve any new documents. In Section 3, we present our algorithm for approximate content summary construction that overcomes these problems and, as we will see, produces content summaries of higher quality than those produced by QBS-Ord and QBS-Lrd.

2.3 Focused Probing for Database Classification

Another way to characterize the contents of a text database is to classify it in a Yahoo!-like hierarchy of topics according to the type of the documents that it contains. For example, CANCERLIT can be classified under the category
“Health,” since it contains mainly health-related documents. Gravano et al. [2003] presented a method to automate the classification of web-accessible text databases, based on focused probing.

The rationale behind this method is that queries closely associated with a topical category retrieve mainly documents about that category. For example, a query [breast cancer] is likely to retrieve mainly documents that are related to the “Health” category. Gravano et al. [2003] automatically construct these topic-specific queries using document classifiers, derived via supervised machine learning. By observing the number of matches generated for each such query at a database, we can place the database in a classification scheme. For example, if one database generates a large number of matches for queries associated with the “Health” category and only a few matches for all other categories, we might conclude that this database should be under category “Health.” If the database does not return the number of matches for a query or does so unreliably, we can still classify the database by retrieving and classifying a sample of documents from the database. Gravano et al. [2003] showed that sample-based classification has both lower accuracy and higher cost than an algorithm that relies on the number of matches; however, in the absence of reliable matching statistics, classifying the database based on a document sample is a viable alternative.

To classify a database, the algorithm in Gravano et al. [2003] (see Figure 1) starts by first sending those query probes associated with subcategories of the top node $C$ of the topic hierarchy, and extracting the number of matches for each probe, without retrieving any documents. Based on the number of matches for the probes for each subcategory $C_i$, the classification algorithm then calculates two metrics, the \textit{Coverage}(D, C_i) and \textit{Specificity}(D, C_i) for the subcategory: \textit{Coverage}(D, C_i) is the absolute number of documents in $D$ that are estimated to belong to $C_i$, while \textit{Specificity}(D, C_i) is the fraction of documents in $D$ that are estimated to belong to $C_i$. The algorithm decides to classify $D$ into a category $C_i$ if the values of \textit{Coverage}(D, C_i) and \textit{Specificity}(D, C_i) exceed two prespecified thresholds $\tau_{ec}$ and $\tau_{es}$, respectively. These thresholds are
determined by “editorial” decisions on how “coarse” a classification should be. For example, higher levels of the specificity threshold $\tau_{es}$ result in assignments of databases mostly to higher levels of the hierarchy, while lower values tend to assign the databases to nodes closer to the leaves.\footnote{Gravano et al. [2003] suggest that $\tau_{ec} \approx 10$ and $\tau_{es} \approx 0.3 - 0.4$ work well for the task of database classification.} When the algorithm detects that a database satisfies the specificity and coverage requirement for a subcategory $C_i$, it proceeds recursively in the subtree rooted at $C_i$. By not exploring other subtrees that did not satisfy the coverage and specificity conditions, the algorithm avoids exploring portions of the topic space that are not relevant to the database.

Next, we introduce a novel technique for constructing content summaries that are highly accurate and efficient to build. Our new technique builds on the document sampling approach used by the QBS algorithms [Callan and Connell 2001] and on the text-database classification algorithm from Gravano et al. [2003]. Just like QBS, which we summarized in Section 2.2, our new technique probes the databases and retrieves a small document sample to construct the approximate content summaries. The classification algorithm, which we summarized in this section, provides a way to focus on those topics that are most representative of a given database’s contents, resulting in accurate and efficiently extracted content summaries.

3. CONSTRUCTING APPROXIMATE CONTENT SUMMARIES

We now describe our algorithm for constructing content summaries for a text database. Our algorithm exploits a topic hierarchy to adaptively send focused probes to the database (Section 3.1). Our technique retrieves a “biased” sample containing documents that are representative of the database contents. Furthermore, our algorithm exploits the number of matches reported for each query to estimate the absolute document frequencies of words in the database (Section 3.2).

3.1 Classification-Based Document Sampling

Our algorithm for approximate content summary construction exploits a topic hierarchy to adaptively send focused probes to a database. These queries tend to efficiently produce a document sample that is representative of the database contents, which leads to highly accurate content summaries. Furthermore, our algorithm classifies the databases along the way. In Section 4, we will show that we can exploit categorization to improve further the quality of both the generated content summaries and the database selection decisions.

Our content summary construction algorithm is based on the classification algorithm from Gravano et al. [2003], an outline of which we presented in Section 2.3 (see Figure 1). Our content summary construction algorithm is shown in Figure 2. The main difference with the classification algorithm is that we exploit the focused probing to retrieve a document sample. We have enclosed in boxes those portions directly relevant to content summary extraction. Specifically, for
each query probe, we retrieve $k$ documents from the database in addition to the number of matches that the probe generates (box $\beta$ in Figure 2). Also, we record two sets of word frequencies based on the probe results and extracted documents (boxes $\beta$ and $\gamma$). These two sets are described next.

1. $df(w)$ is the actual number of documents in the database that contain word $w$. The algorithm knows this number only if $[w]$ is a single-word query probe that was issued to the database.\textsuperscript{8}

2. $sf(w)$ is the number of documents in the extracted sample that contain word $w$.

The basic structure of the probing algorithm is as follows. We explore (and send query probes for) only those categories with sufficient specificity and coverage, as determined by the $\tau_{es}$ and $\tau_{ec}$ thresholds (for details, see Section 2.3). As a result, this algorithm categorizes the databases into the classification scheme during probing. We will exploit this categorization to improve the quality of the generated content summaries in Section 4.2.

Figure 3 illustrates how our algorithm works for the CNN Sports Illustrated database, a database with articles about sports, and for a toy hierarchical scheme with four categories under the root node: “Sports,” “Health,”

\textsuperscript{8}The number of matches reported by a database for a single-word query $[w]$ might differ slightly from $df(w)$, for example, if the database applies stemming [Salton and McGill 1983] to query words so that a query [computers] also matches documents with word “computer.”
“Computers,” and “Science.” We pick specificity and coverage thresholds $\tau_{es} = 0.4$ and $\tau_{ec} = 10$, respectively, which work well for the task of database classification [Gravano et al. 2003]. The algorithm starts by issuing query probes associated with each of the four categories. The “Sports” probes generate many matches (e.g., query [baseball] matches 24,520 documents). In contrast, probes for the other sibling categories (e.g., [metallurgy] for category “Science”) generate just a few or no matches. The Coverage of category “Sports” is the sum of the number of matches for its probes, or 32,050. The Specificity of category “Sports” is the fraction of matches that correspond to “Sports” probes, or 0.967. Hence, “Sports” satisfies the Specificity and Coverage criteria (recall that $\tau_{es} = 0.4$ and $\tau_{ec} = 10$) and is further explored in the next level of the hierarchy. In contrast, “Health,” “Computers,” and “Science” are not considered further. By pruning the probe space, we improve the efficiency of the probing process by giving attention to the topical focus (or foci) of the database. (Out-of-focus probes would tend to return few or no matches.)

During probing, our algorithm retrieves the top-$k$ documents returned by each query (box $\beta$ in Figure 2). For each word $w$ in a retrieved document, the algorithm computes $sf(w)$ by measuring the number of documents in the sample, extracted in a probing round, that contain $w$. If a word $w$ appears in document samples retrieved during later phases of the algorithm for deeper levels of the hierarchy, then all $sf(w)$ values are added together (the merge step in box $\gamma$).
Similarly, during probing, the algorithm keeps track of the number of matches produced by each single-word query \([w]\). As discussed, the number of matches for such a query is (an approximation of) the \(df(w)\) frequency (i.e., the number of documents in the database with word \(w\)). These \(df(\cdot)\) frequencies are crucial to estimate the absolute document frequencies of all words that appear in the document sample extracted, as discussed next.

3.2 Estimating Absolute Document Frequencies

The QBS-Ord and QBS-Lrd techniques return the frequency of words in the document sample (i.e., the \(sf(\cdot)\) frequencies), with no absolute frequency information. We now show how we can exploit the \(df(\cdot)\) and \(sf(\cdot)\) document frequencies that we extract from a database to build a content summary for the database with accurate absolute document frequencies.

Before turning to the details of the algorithm, we describe a (simplified) example in Figure 4 to introduce the basic intuition behind our approach. After probing the CANCERLIT database using the algorithm in Figure 2, we rank all words in the extracted documents according to their \(sf(\cdot)\) frequency. For example, “cancer” has the highest \(sf(\cdot)\) value and “hepatitis” the lowest such value in Figure 4. The \(sf(\cdot)\) value of each word is denoted by an associated vertical bar. Also, the figure shows the \(df(\cdot)\) frequency of each word that appeared as a single-word query. For example, \(df(hepatitis) = 200,000\), because query probe [hepatitis] returned 200,000 matches. Note that the \(df\) value of some words (e.g., “stomach”) is unknown. These words are in documents retrieved during probing, but did not appear as single-word probes. Finally, note from the figure

\[ f = P(r \cdot p) \]
that \( sf(\text{hepatitis}) \approx sf(\text{stomach}) \), and so we might want to estimate \( df(\text{stomach}) \) to be close to the (known) value of \( df(\text{hepatitis}) \).

To specify how to “propagate” the known \( df \) frequencies to “nearby” words with similar \( sf \) frequencies, we exploit well-known laws on the distribution of words over text documents. Zipf \[1949\] was the first to observe that word-frequency distributions follow a power law, an observation later refined by Mandelbrot \[1988\]. Mandelbrot identified a relationship between the rank \( r \) and the frequency \( f \) of a word in a text database, \( f = P(r + p)^B \), where \( P, B, \) and \( p \) are database-specific parameters (\( P > 0, B < 0, p \geq 0 \)). This formula indicates that the most frequent word in a collection (i.e., the word with rank \( r = 1 \)) will tend to appear in about \( P(1 + p)^B \) documents, while, say, the tenth most frequent word will appear in just about \( P(10 + p)^B \) documents. Therefore, given Mandelbrot’s formula for the database and the word ranking, we can estimate the frequency of each word.

Our technique relies on Mandelbrot’s formula to define the content summary of a database and consists of two steps, detailed next.

1. During probing, exploit the \( sf(\cdot) \) frequencies derived during sampling to estimate the rank-frequency distribution of words over the entire database (Section 3.2.1).
2. After probing, exploit the \( df(\cdot) \) frequencies obtained from one-word query probes to estimate the rank of these words in the actual database; then, estimate the document frequencies of all words by “propagating” the known rank and document frequencies to “nearby” words \( w \) for which we only know \( sf(w) \) and not \( df(w) \) (Section 3.2.2).

### 3.2.1 Estimating the Word Rank-Frequency Distribution.

The first part of our technique estimates the parameters \( P \) and \( B \) (of a slightly simplified version\(^{10}\)) of Mandelbrot’s formula for a given database. To do this, we examine how the parameters of Mandelbrot’s formula change for different sample sizes. We observed that in all the databases that we examined for our experiments, \( \log(P) \) and \( B \) tend to increase logarithmically with the sample size \( |S| \). (This is actually an effect of sampling from a power-law distribution [Baayen 2006].)

Specifically,

\[
\log(P) = P_1 \log(|S|) + P_2 \tag{1a}
\]

\[
B = B_1 \log(|S|) + B_2 \tag{1b}
\]

and \( P_1, P_2, B_1, \) and \( B_2 \) are database-specific constants, independent of sample size.

Based on the preceding empirical observations, we proceed as follows for a database \( D \). At different points during the document sampling process, we calculate \( P \) and \( B \). After sampling, we use regression to estimate the values of \( P_1, P_2, B_1, \) and \( B_2 \). We also estimate the size of database \( D \) using the sample-resample method [Si and Callan 2003] with five resampling queries. Finally, we

\(^{10}\)For numerical stability, we define \( f = Pr^B \), which allows us to use linear regression in the log-log space to estimate parameters \( P \) and \( B \).
compute the values of $P$ and $B$ for the database by substituting the estimated $|D|$ for $|S|$ in Eqs. (1a) and (1b). At this point, we have a description of the frequency-rank distribution for the actual database.

### 3.2.2 Estimating Document Frequencies

Given the parameters of Mandelbrot’s formula, the actual document frequency $df(w)$ of each word $w$ can be derived from its rank in the database. For high-frequency words, the rank in the sample is usually a good approximation of the rank in the database. Unfortunately, this is rarely the case for low-frequency words, for which we rely on the observation that the $df(\cdot)$ frequencies derived from one-word query probes can help estimate the rank and $df(\cdot)$ frequency of all words in the database. Our rank and frequency estimation algorithm works as follows.

**Algorithm.**

1. Sort words in descending order of their $sf(\cdot)$ frequencies to determine the sample rank $sr(w_i)$ of each word $w_i$; do not break ties for words with equal $sf(\cdot)$ frequency and assign the same sample rank $sr(\cdot)$ to these words.
2. For each word $w$ in a one-word query probe ($df(w)$ is known), use Mandelbrot’s formula and compute the database rank $ar(w) = \left(\frac{df(w)}{P}\right)^{\frac{1}{B}}$.
3. For each word $w$ not in a one-word query probe ($df(w)$ is unknown), do the following.
   a. Find two words $w_1$ and $w_2$ with known $df$ and consider their ranks in the sample (i.e., $sr(w_1)$, $sr(w_2)$) and in the database (i.e., $ar(w_1)$, $ar(w_2)$).
   b. Use interpolation in the log-log space to compute the database rank $ar(w)$.
   c. Use Mandelbrot’s formula to compute $\hat{df}(w) = P \cdot ar(w)^B$, where $ar(w)$ is the rank of word $w$ as computed in the previous step.

Using the aforesaid procedure, we can estimate the $df$ frequency of each word that appears in the sample.

**Example 3.1.** Consider the medical database CANCERLIT and Figure 4. We know that $df(liver) = 1,400,000$ and $df(hepatitis) = 200,000$, since the respective one-word queries reported as many matches. Furthermore, the ranks of the two words in the sample are $sr(liver) = 4$ and $sr(hepatitis) = 10$, respectively. While we know that the rank of the word “kidneys” in the sample is $sr(kidneys) = 8$, we do not know $df(kidneys)$ because [kidneys] was not a query probe. However, the known values of $df(hepatitis)$ and $df(liver)$ can help us estimate the rank of “kidneys” in the database and, in turn, the $df(kidneys)$ frequency. For the CANCERLIT database, we estimate that $P = 6 \cdot 10^6$ and $B = -1.15$. Thus, we estimate that “liver” is the fourth most frequent word in the database (i.e., $ar(liver) = 4$), while “hepatitis” is ranked number 20 (i.e., $ar(hepatitis) = 20$). Therefore, 15 words in the database are ranked between “liver” and “hepatitis”, while in the sample there are only 5 such words. By exploiting this observation and by interpolation, we estimate that “kidneys” (with rank 8 in the sample) is the 14th most frequent word in the database. Then, using the rank information with Mandelbrot’s formula, we compute $\hat{df}(kidneys) = 6 \cdot 10^8 \cdot 14^{-1.15} \approx 288,472$.

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$^{11}$It is preferable, but not essential, to pick $w_1$ and $w_2$ such that $sr(w_1) < sr(w) < sr(w_2)$.

$^{12}$The exact formula is $ar(w) = \exp(\frac{\ln(sr(w_1)) + \ln(ar(w_1)) + \ln(sr(w_2)) + \ln(ar(w_2))}{\ln(ar(w_1))})$. 

During sampling, we also send to the database query probes that consist of more than one word. (Recall that our query probes are derived from an underlying automatically learned document classifier.) We do not exploit multiword queries for determining the \(df\) frequencies of their words, since the number of matches returned by a Boolean-AND multiword query is only a lower bound on the \(df\) frequency of each intervening word. However, the average length of the query probes that we generate is small (less than 1.5 words in our experiments), and their median length is 1. Hence, the majority of the query probes provide us with \(df\) frequencies that we can exploit.

Finally, a potential problem with the current algorithm is that it relies on the database reporting a value for the number of matches for a one-word query \(w\) that is equal (or at least close) to the value of \(df(w)\). Sometimes, however, these two values might differ (e.g., if a database applies stemming to query words). In this case, frequency estimates might not be reliable. However, it is rather easy to detect such configurations [Meng et al. 1999] and adapt the frequency estimation algorithm properly. For example, if we detect that a database uses stemming, we might decide to compute the frequency and rank of each word in the sample after the application of stemming and then adjust the algorithms accordingly.

In summary, we have presented a novel technique for estimating the absolute document frequency of the words in a database. As we will see, this technique produces relatively accurate frequency estimates for the words in a document sample of the database. However, database words that are not in the sample documents in the first place are ignored and not made part of the resulting content summary. Unfortunately, any document sample of moderate size will necessarily miss many words that occur only a small number of times in the associated database. The absence of these words from the content summaries can negatively affect the performance of database selection algorithms for queries that mention such words. To alleviate this sparse-data problem, we exploit the observation that incomplete content summaries of topically related databases can be used to complement each other, as discussed next.

4. DATABASE SELECTION WITH SPARSE CONTENT SUMMARIES

So far, we have discussed how to efficiently construct approximate content summaries using document sampling. However, any efficient algorithm for constructing content summaries through query probes is likely to produce incomplete content summaries, which can adversely affect the effectiveness of the database selection process. To alleviate this sparse-data problem, we exploit the observation that incomplete content summaries of topically related databases can be used to complement each other. In this section, we present two alternative algorithms that exploit this observation and make database selection more resilient to incomplete content summaries. Our first algorithm (Section 4.1) selects databases hierarchically, based on categorization of the databases. Our second algorithm (Section 4.2) is a flat selection strategy that exploits the database categorization implicitly by using shrinkage, and enhances the database content summaries with category-specific words that appear in topically similar databases.
4.1 Hierarchical Database Selection

We now introduce a hierarchical database selection algorithm that exploits the database categorization and content summaries to alleviate the negative effect of incomplete content summaries. This algorithm consists of two basic steps, given next.

Algorithm.

1. “Propagate” the database content summaries to the categories of the hierarchical classification scheme and create the associated category content summaries using Definition 4.1.
2. Use the content summaries of categories and databases to perform database selection hierarchically by zooming in on the most relevant portions of the topic hierarchy.

The intuition behind our approach is that databases classified under similar topics tend to have similar vocabularies. (We present supporting experimental evidence for this statement in Section 6.2.) Hence, we can view the (potentially incomplete) content summaries of all databases in a category as complementary, and exploit this for better database selection. For example, consider the CANCER.gov database and its associated content summary in Figure 5. As we can see, CANCER.gov was correctly classified under “Cancer” by the algorithm of Section 3.1. Unfortunately, the word “metastasis” did not appear in any of the documents extracted from CANCER.gov during probing, so this word is missing from the content summary. However, we see that CancerBACUP\(^\text{13}\), another database classified under “Cancer”, has \(\hat{df}(\text{metastasis}) = 3,569\), a relatively high value. Hence, we might conjecture that the word “metastasis” is an important word for all databases in the “Cancer” category and that this word did not appear in CANCER.gov because it was not discovered during sampling, and not because it does not occur in the database. Therefore, we can create a content summary with category “Cancer” in such a way that the word “metastasis” appears with relatively high frequency. This summary is obtained by merging the summaries of all databases under the category.

In general, we define the content summary of a category as follows.

\textbf{Definition 4.1.} Consider a category \(C\) and the set \(db(C) = \{D_1, \ldots, D_n\}\) of databases classified (not necessarily immediately) under \(C\).\(^\text{14}\) The \textit{approximate content summary} \(\hat{S}(C)\) of category \(C\) contains, for each word \(w\), an estimate \(\hat{p}(w|C)\) of \(p(w|C)\), where \(p(w|C)\) is the probability that a randomly selected document from a database in \(db(C)\) contains the word \(w\). The \(\hat{p}(w|C)\) estimates in \(\hat{S}(C)\) are derived from the approximate content summaries of the databases.

\(^\text{13}\)http://www.cancerbacup.org.uk
\(^\text{14}\)If a database \(D_i\) is classified under multiple categories, we can treat \(D_i\) as multiple disjoint subdatabases, with each subdatabase being associated with one of the \(D_i\) categories and containing only the documents in the respective category.

Fig. 5. Associating content summaries with categories.

in $db(C)$ as\(^\text{15}\)

\[
\hat{p}(w|C) = \frac{\sum_{D \in db(C)} \hat{p}(w|D) \cdot |D|}{\sum_{D \in db(C)} |D|}, \quad (2)
\]

where $|D|$ is an estimate of the number of documents in $D$ (see Definition 2.3).\(^\text{16}\)

The approximate content summary $\hat{S}(C)$ also includes:

— the number of databases $|db(C)|$ under $C$ ($n$ in this definition);
— an estimate $|\hat{C}| = \sum_{D \in db(C)} |D|$ of the number of documents in all databases under $C$; and

\(^{15}\)An alternative is to define $\hat{p}(w|C) = \frac{\sum_{D \in db(C)} \hat{p}(w|D)}{|db(C)|}$, which “weights” each database equally, regardless of its size. We implemented this alternative and obtained results virtually identical to those for Eq. (2).

\(^{16}\)We estimate the number of documents in the database as described in Section 3.2.1.
Selecting the $K$ most specific databases for a query hierarchically.

---

For each word $w$, an estimate $\hat{df}_C(w)$ of the total number of documents under $C$ that contain the word $w$: $\hat{df}_C(w) = \hat{p}(w|C) \cdot |\hat{C}|$.

By having content summaries associated with categories in the topic hierarchy, we can select databases for a query by proceeding hierarchically from the root category. At each level, we use existing flat database algorithms such as CORI [Callan et al. 1995] or bGlOSS [Gravano et al. 1999]. These algorithms assign a score to each database (or category, in our case) that specifies how promising the database (or category) is for the query, as indicated by the content summaries (see Example 2.2). Given the scores for categories at one level of the hierarchy, the selection process continues recursively down the most promising subcategories. As further motivation for our approach, earlier research has indicated that distributed information retrieval systems tend to produce better results when documents are organized in topically cohesive clusters [Xu and Croft 1999; Larkey et al. 2000].

Figure 6 specifies our hierarchical database selection algorithm in detail. The algorithm receives as input a query and the target number of databases $K$ that we are willing to search for the query. Also, the algorithm receives the top category $C$ as input, and starts by invoking a flat database selection algorithm to score all subcategories of $C$ for the query (step 1), using the content summaries associated with the subcategories. We assume in our discussion that the scores produced by the database selection algorithms are greater than or equal to zero, with a zero score indicating that a database or category should be ignored for the query. If at least one promising subcategory has a nonzero score (step 2), then the algorithm picks the best such subcategory $C_j$ (step 3). If $C_j$ has $K$ or more databases under it (step 4), the algorithm proceeds recursively under that branch only (step 5). This strategy privileges “topic-specific” databases over those with broader scope. On the other hand, if $C_j$ does not have sufficiently many (i.e., $K$ or more) databases (step 6), then intuitively the algorithm has gone as deep in the hierarchy as possible (exploring only category $C_j$ would result in fewer than $K$ databases being returned). Then, the algorithm returns all $|db(C_j)|$ databases under $C_j$, plus the best $K - |db(C_j)|$ databases under $C$ but not in $C_j$, according to the flat database selection algorithm of choice (step 7). If no subcategory of $C$ has a nonzero score (step 8), then again this indicates that the execution has gone as deep in the hierarchy as possible. Therefore, we
Fig. 7. Exploiting a topic hierarchy for database selection.

return the best $K$ databases under $C$, according to the flat database selection algorithm (step 9).

Figure 7 shows an example of an execution of this algorithm for query [babe ruth] and for a target of $K = 3$ databases. The top-level categories are evaluated by a flat database selection algorithm for the query, and the “Sports” category is deemed best, with a score of 0.93. Since the “Sports” category has more than three databases, the query is “pushed” into this category. The algorithm proceeds recursively by pushing the query into the “Baseball” category. If we had initially picked $K = 10$ instead, the algorithm would have still picked “Sports” as the first category to explore. However, “Baseball” has only seven databases, so the algorithm picks them all, and chooses the best three databases under “Sports” to reach the target of ten databases for the query.

In summary, our hierarchical database selection algorithm attempts to choose the most specific databases for a query. By exploiting the database categorization, this hierarchical algorithm manages to compensate for the necessarily incomplete database content summaries produced by query probing. However, by first selecting the most appropriate categories, this algorithm might miss some relevant databases that are not under the selected categories. One solution would be to try different hierarchy-traversal strategies that could lead to the selection of databases from multiple branches of the hierarchy. Instead of following this direction of finding the appropriate traversal strategy, we opt for an alternative, flat selection scheme: We use the classification hierarchy only for improving the extracted content summaries, and we allow the database selection algorithm to choose among all available databases. Next, we describe this approach in detail.

4.2 Shrinkage-Based Database Selection

As argued previously, content summaries built from relatively small document samples are inherently incomplete, which might affect the performance of database selection algorithms that rely on such summaries. Now, we show how we can exploit database category information to improve the quality of the
database summaries, and subsequently the quality of database selection decisions. Specifically, Section 4.2.1 presents an overview of our general approach, which builds on the shrinkage ideas from document classification [McCallum et al. 1998], while Section 4.2.2 explains in detail how we use shrinkage to construct content summaries. Finally, Section 4.2.3 presents a database selection algorithm that uses the shrinkage-based content summaries in an adaptive and query-specific way.

4.2.1 Overview of our Approach. In Sections 2.2 and 3.1, we discussed sampling-based techniques for building content summaries from hidden-web text databases, and argued that low-frequency words tend to be absent from these summaries. Additionally, other words might be disproportionately represented in the document samples. One way to alleviate these problems is to increase the document sample size. Unfortunately, this solution might be impractical, since it would involve extensive querying of (remote) databases. Even more importantly, increases in document sample size do not tend to result in comparable improvements in content summary quality [Callan and Connell 2001]. An interesting challenge is thus to improve the quality of approximate content summaries, without necessarily increasing the document sample size.

This challenge has a counterpart in the problem of hierarchical document classification. Document classifiers rely on training data to associate words with categories. Often, only limited training data is available, which might lead to poor classifiers. Classifier quality can be increased with more training data, but creating large numbers of training examples might be prohibitively expensive. As a less expensive alternative, McCallum et al. [1998] suggested sharing training data across related topic categories. Specifically, their shrinkage approach compensates for sparse training data for a category by using training examples for more general categories. For example, the training documents for the “Heart” category can be augmented with those from the more general “Health” category. The intuition behind this approach is that the word distribution in “Health” documents is hopefully related to that in the “Heart” documents.

We can apply the same shrinkage principle to our problem, which requires that databases be categorized into a topic hierarchy. This categorization might be an existing one (e.g., if the databases are classified under Open Directory17). Alternatively, databases can be classified automatically using the classification algorithm briefly reviewed in Section 2.3. Regardless of how databases are categorized, we can exploit this categorization to improve content summary coverage. The key intuition behind the use of shrinkage in this context is that databases under similar topics tend to have related content summaries. Hence, we can use the approximate content summaries for similarly classified databases to complement each other, as illustrated in the following example.

Example 4.2. Figure 8 shows a fraction of a classification scheme with two text databases \(D_1\) and \(D_2\) classified under “Heart,” and one text database \(D_3\) classified under the (higher-level) category “Health.” Assume that the approximate content summary of \(D_1\) does not contain the word “hypertension,”

\[\text{http://www.dmoz.org}\]
but that this word appears in many documents in $D_1$. (“Hypertension” might not have appeared in any of the documents sampled to build $\hat{S}(D_1)$.) In contrast, “hypertension” appears in a relatively large fraction of $D_2$ documents as reported in the content summary of $D_2$, which is also classified under the “Heart” category. Then, by “shrinking” $\hat{p}(\text{hypertension}|D_1)$ towards the value of $\hat{p}(\text{hypertension}|D_2)$, we can capture more closely the actual (and unknown) value of $p(\text{hypertension}|D_1)$. The new, “shrunk” value is, in effect, exploiting documents sampled from both $D_1$ and $D_2$.

We expect databases under the same category to have similar content summaries. Furthermore, even databases classified under relatively general categories can help improve the approximate content summary of a more specific database. Consider database $D_3$, classified under “Health” in Figure 8. Here $\hat{S}(D_3)$ can help complement the content summary approximation of databases $D_1$ and $D_2$, which are classified under a subcategory of “Health,” namely “Heart.” Database $D_3$, however, is a more general database that contains documents in topics other than heart-related. Hence, the influence of $\hat{S}(D_3)$ on $\hat{S}(D_1)$ should perhaps be less than that of, say, $\hat{S}(D_2)$. In general, and just as for document classification [McCallum et al. 1998], each category level might be assigned a different “weight” during shrinkage. We discuss this and other specific aspects of our technique next.

4.2.2 Using Shrinkage over a Topic Hierarchy. We now define more formally how we can use shrinkage for content summary construction. For this, we use the notion of content summaries for the categories of a classification scheme (Definition 4.1) from Section 4.1.
Creating shrunk content summaries. Section 4.2.1 argued that mixing information from content summaries of topically related databases may lead to more complete approximate content summaries. We now formally describe how to use shrinkage for this purpose. In essence, we create a new content summary for each database $D$ by shrinking the approximate content summary of $D$, $\hat{S}(D)$, so that it is “closer” to the content summaries $S(C_i)$ of each category $C_i$ under which $D$ is classified.

**Definition 4.3.** Consider a database $D$ classified under categories $C_1, \ldots, C_m$ of a hierarchical classification scheme, with $C_i = \text{Parent}(C_{i+1})$ for $i = 1, \ldots, m - 1$. Let $C_0$ be a dummy category whose content summary $\hat{S}(C_0)$ contains the same estimate $\hat{p}(w|C_0)$ for every word $w$. Then, the shrunk content summary $\hat{R}(D)$ of database $D$ consists of:

— an estimate $|D|$ of the number of documents in $D$; and
— for each word $w$, a shrinkage-based estimate $\hat{p}_R(w|D)$ of $p(w|D)$, defined as

$$
\hat{p}_R(w|D) = \lambda_{m+1} \cdot \hat{p}(w|D) + \sum_{i=0}^{m} \lambda_i \cdot \hat{p}(w|C_i)
$$

(3)

for a choice of $\lambda_i$ values such that $\sum_{i=0}^{m+1} \lambda_i = 1$ (see next).

As described so far, the $\hat{p}(w|C_i)$ values in the $\hat{S}(C_i)$ content summaries are not independent of each other: Since $C_i = \text{Parent}(C_{i+1})$, all the databases under $C_{i+1}$ are also used to compute $\hat{S}(C_i)$, by Definition 4.1. To avoid this overlap, before estimating $\hat{R}(D)$, we subtract from $\hat{S}(C_i)$ all the data used to construct $\hat{S}(C_{i+1})$. Also note that a simple version of Eq. (3) is used for database selection based on language models [Si et al. 2002]. Language model database selection “smoothes” the $\hat{p}(w|D)$ probabilities with the probability $\hat{p}(w|G)$ for a “global” category $G$. Our technique extends this principle and does multilevel smoothing of $\hat{p}(w|D)$, using the hierarchical classification of $D$. We now describe how to compute the $\lambda_i$ weights used in Eq. (3).

**Calculating category mixture weights.** We define the $\lambda_i$ mixture weights from Eq. (3), so as to make the shrunk content summaries $\hat{R}(D)$ for each database $D$ as similar as possible to both the starting summary $\hat{S}(D)$ and the summary $\hat{S}(C_i)$ of each category $C_i$ under which $D$ is classified. Specifically, we use expectation maximization (EM) [McCallum et al. 1998] to calculate the $\lambda_i$ weights, using the algorithm in Figure 9. (This is a simple version of the EM algorithm from Dempster et al. [1977].)

The Expectation step calculates the likelihood that content summary $\hat{R}(D)$ corresponds to each category. The Maximization step weights the $\lambda_i$’s to maximize the total likelihood across all categories. The result of the algorithm is the shrunk content summary $\hat{R}(D)$, which incorporates information from multiple content summaries and is thus hopefully closer to the complete (and unknown) content summary $S(D)$ of database $D$.

For illustration purposes, Table II reports the computed mixture weights for two databases that we used in our experiments. As we can see, in both cases the original database content summary and that of the most specific category
Fig. 9. Using expectation maximization to determine the $\lambda_i$ mixture weights for the shrunk content summary of a database $D$. for the database receive the highest weights (0.421 and 0.414, respectively, for the AIDS.org database, and 0.411 and 0.297, respectively, for the American Economics Association database). However, higher-level categories also receive nonnegligible weights. In general, the $\lambda_{m+1}$ weight associated with a database (as opposed to with the categories under which it is classified) is usually highest among the $\lambda_i$’s, and so the word-distribution statistics for the database are not eclipsed by the category statistics. (We verify this claim experimentally in Section 6.3.)

Shrinkage might in some cases (incorrectly) reduce the estimated frequency of words that distinctly appear in a database. Fortunately, this reduction tends to be small because of the relatively high value of $\lambda_{m+1}$, and hence these distinctive words remain with high frequency estimates. As an example, consider the AIDS.org database from Table II. The word chlamydia appears in 3.5% of those in the AIDS.org database. This word appears in 4% of the documents in the document sample from AIDS.org and in approximately 2% of those in the content summary for the AIDS category. After applying shrinkage, the estimated frequency of the word chlamydia is somewhat reduced, but still high. The shrinkage-based estimate is that chlamydia appears in 2.85% of the documents in AIDS.org, which is still close to the real frequency.


<table>
<thead>
<tr>
<th>Database</th>
<th>Category</th>
<th>$\lambda$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Uniform</td>
<td>0.075</td>
<td></td>
</tr>
<tr>
<td>Root</td>
<td>0.026</td>
<td></td>
</tr>
<tr>
<td>Health</td>
<td>0.061</td>
<td></td>
</tr>
<tr>
<td>Diseases</td>
<td>0.003</td>
<td></td>
</tr>
<tr>
<td>AIDS</td>
<td>0.414</td>
<td></td>
</tr>
<tr>
<td>AIDS.org</td>
<td>0.421</td>
<td></td>
</tr>
</tbody>
</table>

Shrinkage might in some cases (incorrectly) cause inclusion of words in the content summary that do not appear in the corresponding database. Fortunately, such spurious words tend to be introduced in summaries with low weight. Using once again the AIDS.org database as an example, we observed that the word metastasis was (incorrectly) added by the shrinkage process to the summary: Metastasis does not appear in the database, but is included in documents in other databases under the Health category and hence is in the Health category content summary. The shrunk content summary for AIDS.org estimates that metastasis appears in just 0.03% of the database documents, so such a low estimate is unlikely to adversely affect database selection decisions. (We will evaluate the positive and negative effects of shrinkage experimentally later, in Sections 6 and 7.)

Finally, note that the $\lambda_i$ weights are computed offline for each database when the sampling-based database content summaries are created. This computation does not involve any overhead at query-processing time.

4.2.3 Improving Database Selection Using Shrinkage. So far, we introduced a shrinkage-based strategy to complement the incomplete content summary of a database with the summaries of topically related databases. In principle, existing database selection algorithms could proceed without modification and use the shrunk summaries to assign scores for all queries and databases. However, sometimes shrinkage might not be beneficial and should not be used. Intuitively, shrinkage should be used to determine the score $s(q, D)$ for a query $q$ and a database $D$ only if the uncertainty associated with this score would otherwise be large.

The uncertainty associated with an $s(q, D)$ score depends on a number of sample-, database-, and query-related factors. An important factor is the size of the document sample relative to that of database $D$. If an approximate summary $\hat{S}(D)$ was derived from a sample that included most of the documents in $D$, then this summary is already “sufficiently complete.” (For example, this situation might arise if $D$ is a small database.) In this case, shrinkage is not necessary and might actually be undesirable, since it might introduce spurious words into the content summary from topically related (but not identical) databases. Another factor is the frequency of query words in the sample used to determine $\hat{S}(D)$. If, say, every word in a query appears in nearly all sample documents and the sample is representative of the entire database contents, then there is little uncertainty on the distribution of the words over the database at large. Therefore, the uncertainty about the score assigned to the database
from the database selection algorithm is also low, and there is no need to apply shrinkage. Analogously, if every query word appears in only a small fraction of sample documents, then most probably the database selection algorithm would assign a low score to the database, since it is unlikely that the database is a good candidate for evaluating the query. Again, in this case shrinkage would provide limited benefit and should be avoided. However, consider the following scenario, involving bGIOSS and a multiword query for which most words appear very frequently in the sample, but where one query word is missing from the document sample altogether. In this case, bGIOSS would assign a zero score to the database. The missing word, though, may have a nonzero frequency in the complete content summary, and the score assigned by bGIOSS to the database would have been significantly higher in the presence of this knowledge because of bGIOSS’s Boolean nature. So, the uncertainty about the database score that bGIOSS would assign if given the complete summary is high, and it is thus desirable to apply shrinkage. In general, for query-word distribution scenarios where the approximate content summary is not sufficient to reliably establish the query-specific score for a database, shrinkage should be used.

More formally, consider a query \( q = [w_1, \ldots, w_n] \) with \( n \) words \( w_1, \ldots, w_n \), a database \( D \), and an approximate content summary for \( D \), \( \hat{S}(D) \), derived from a random sample \( S \) of \( D \). Furthermore, suppose that word \( w_k \) appears in exactly \( s_k \) documents in the sample \( S \). For every possible combination of values \( d_1, \ldots, d_n \) (see the following), we compute:

— the probability \( P \) that \( w_k \) appears in exactly \( d_k \) documents in \( D \), for \( k = 1, \ldots, n \), as

\[
P = \prod_{k=1}^{n} \frac{d_k^\gamma (d_k | D |)^{s_k} \left( 1 - \frac{d_k}{|D|} \right)^{|S| - s_k}}{\sum_{i=0}^{|D|} i^\gamma \cdot \left( \frac{i}{|D|} \right)^{s_k} \left( 1 - \frac{i}{|D|} \right)^{|S| - s_k}}, \tag{4}
\]

where \( \gamma \) is a database-specific constant (for details, see Appendix A); and

— the score \( s(q, D) \) that the database selection algorithm of choice would assign to \( D \) if \( p(w_k | D) = \frac{d_k}{|D|} \), for \( k = 1, \ldots, n \).

So for each possible combination of values \( d_1, \ldots, d_n \), we compute both the probability of the value combination and the score that the database selection algorithm would assign to \( D \) for this document frequency combination. Then, we can approximate the uncertainty behind the \( s(q, D) \) score by examining the mean and variance of database scores over the different \( d_1, \ldots, d_n \) values. This computation can be performed efficiently for a generic database selection algorithm: Given the sample frequencies \( s_1, \ldots, s_n \), a large number of possible \( d_1, \ldots, d_n \) values have virtually zero probability of occurring, so we can ignore them. Additionally, mean and variance converge fast, even after examining only a small number of \( d_1, \ldots, d_n \) combinations. Specifically, we examine random \( d_1, \ldots, d_n \) combinations and periodically calculate the mean and variance of the score distribution. Usually, after examining just a few hundred random \( d_1, \ldots, d_n \) combinations, mean and variance converge to a stable value. The mean and variance computation typically requires less than 0.1 seconds for
Fig. 10. Using shrinkage adaptively for database selection.

Input: Query \( q = [w_1, \ldots, w_n] \); databases \( D_1, \ldots, D_m \)

Content Summary Selection step:
For each \( D_i \):

- For every possible choice of values for \( d_1, \ldots, d_n \) (see text):
  - Compute the probability \( P \) that \( w_k \) appears in exactly \( d_k \) documents in \( D_i \), for \( k = 1, \ldots, n \).

  - Compute the score \( s(q, D_i) \) assuming that \( w_k \) appears in exactly \( d_k \) documents in \( D_i \), for \( k = 1, \ldots, n \).

If the standard deviation of the score distribution across \( d_k \) values is larger than its mean then \( A(D_i) = \hat{S}(D_i) \) // use “shrunk” content summary
else \( A(D_i) = \hat{R}(D_i) \) // use “unshrunk” content summary

Scoring step:
For each \( D_i \):

- Compute \( s(q, D_i) \) using the \( A(D_i) \) content summary, as selected in the Content Summary Selection step.

Ranking step:
Rank the databases by decreasing score \( s(q, D_i) \).

In this section, we presented two database selection strategies that exploit database classification to improve selection decisions in the presence of

\[ \text{We measured the time on a PC with a dual AMD Athlon CPU, running at 1.8 GHz.} \]
incomplete content summaries. Next, we present the settings for the experi-
mental evaluation of the content summary construction algorithm of Section 3
and of the database selection algorithms of Section 4.

5. EXPERIMENTAL SETTING
In this section, we describe the data (Section 5.1), strategies for computing con-
tent summaries (Section 5.2), and database selection algorithms (Section 5.3)
that we use for the experiments reported in Sections 6 and 7.

5.1 Datasets
The content summary construction techniques that we proposed before rely on
a hierarchical categorization scheme. For our experiments, we use the classifi-
cation scheme from Gravano et al. [2003], with 72 nodes organized in a 4-level
hierarchy. To evaluate the algorithms described in this article, we use four
datasets in conjunction with the hierarchical classification scheme. These are
as follows.

— **Controlled.** This is a dataset that was also used for evaluating the task of
database classification in Gravano et al. [2003]. To construct this dataset, we
used postings from Usenet newsgroups where the signal-to-noise ratio was
high and where the documents belonged (roughly) to one of the categories
of our classification scheme. For example, the newsgroups `comp.lang.c` and
`comp.lang.c++` were considered relevant to category “C/C++.” We collected
500,000 articles from April through May 2000. Out of these 500,000 articles,
81,000 were used to train and test the document classifiers that we used for
the Focused Probing algorithm (see Section 5.2.1). We removed all headers
from the newsgroup articles, with the exception of the “Subject” line; we
also removed the e-mail addresses contained in the articles. Except for these
modifications, we made no changes to the collected documents.

We used the remaining 419,000 articles to build the 500 databases in the
Controlled dataset. The size of the 500 Controlled databases that we cre-
ated ranges from 25 to 25,000 documents. Out of the 500 databases, 350 are
homogeneous, with documents from a single category, while the remaining
150 are heterogeneous, with a variety of category mixes. We define a data-
base as homogeneous when it has articles from only one node, regardless of
whether this node is a leaf node. If it is not, then it has an equal number
of articles from each leaf node in its subtree. Heterogeneous databases, on
the other hand, have documents from different categories that reside in the
same level in the hierarchy (not necessarily siblings), with different mixture
percentages. We believe that these databases model real-world searchable
web databases, with a variety of sizes and foci.

— **TREC4.** This is a set of 100 databases created using documents from TREC-
4 [Harman 1996] and separated into disjoint databases via clustering using
the $K$-means algorithm as specified in Xu and Croft [1999]. By construction,
the documents in each database are on roughly the same topic.
Table III. Some of the Real Web Databases in the Web Dataset

<table>
<thead>
<tr>
<th>URL</th>
<th>Documents</th>
<th>Classification</th>
</tr>
</thead>
<tbody>
<tr>
<td><a href="http://www.bartleby.com/">http://www.bartleby.com/</a></td>
<td>375,734</td>
<td>Root → Arts → Literature → Texts</td>
</tr>
<tr>
<td><a href="http://java.sun.com/">http://java.sun.com/</a></td>
<td>78,870</td>
<td>Root → Computers → Programming → Java</td>
</tr>
<tr>
<td><a href="http://mathforum.org/">http://mathforum.org/</a></td>
<td>29,602</td>
<td>Root → Science → Mathematics</td>
</tr>
</tbody>
</table>

—TREC6. This is a set of 100 databases created using documents from TREC-6 [Voorhees and Harman 1998] and separated into disjoint databases using the same methodology as for TREC4.

—Web. This set contains the top-5 real web databases from each of the 54 leaf categories of the hierarchy and from each of the 17 internal nodes of the hierarchy19 (except for the root), as ranked in the Google Directory,20 for a total of 315 databases. The size of these databases ranges from 100 to about 376,000 documents. Table III lists four example databases. We used the GNU Foundation’s wget crawler to download the HTML contents of each site, and kept only the text from each file by stripping the HTML tags using the lynx –dump command.

We use the Controlled dataset in Section 6 to extensively test the quality of the generated content summaries and to pick the variation of our probing strategy (from Section 3.1) that we will use for our subsequent experiments in Section 7. We also use the Web dataset in Section 6 to further validate results on the quality of the summaries. Finally, we use the TREC4 and TREC6 datasets, both for examining the quality of the content summaries and for testing the performance of the database selection algorithms in Section 7. (The TREC4 and TREC6 datasets are the only ones in our testbed that include queries and associated relevance judgments.) For indexing and searching the files in all datasets, we used Jakarta Lucene,22 an open-source full-text search engine.

5.2 Content Summary Construction Algorithms

Our experiments evaluate a number of content summary construction techniques, which vary in their underlying document sampling algorithms (Section 5.2.1) and on whether they use shrinkage and absolute frequency estimation (Section 5.2.2).

5.2.1 Sampling Algorithms. We use different sampling algorithms for retrieving the documents based on which we build the approximate content summaries $\hat{S}(D)$ of each database $D$. We now describe the sampling algorithms in detail.

—Query-Based Sampling (QBS). We experimented with the two versions of QBS described in Section 2, namely QBS-Ord and QBS-Lrd. As the initial
dictionary $D$ for these two methods, we used all words in the Controlled databases. Each query retrieves up to 4 previously unseen documents. Sampling stops after retrieving 300 distinct documents. In our experiments, sampling also stops when 500 consecutive queries retrieve no new documents. To minimize the effect of randomness, we run each experiment over 5 QBS document samples for each database and report average results.

—Focused Probing (FPS). We evaluate our Focused Probing technique, which we introduced in Section 3.1, with a variety of underlying document classifiers. The document classifiers are used by Focused Probing to generate the queries sent to the databases. Specifically, we consider the following variations of the Focused Probing technique:

—**FP-RIPPER.** Focused Probing using RIPPER [Cohen 1996] as the base document classifier.

—**FP-C4.5.** Focused Probing using C4.5RULES, which extracts classification rules from decision tree classifiers generated by C4.5 [Quinlan 1992].

—**FP-Bayes.** Focused Probing using naive-Bayes classifiers [Duda et al. 2000] in conjunction with the technique to extract rules from numerically-based naive-Bayes classifiers from Gravano et al. [2003].

—**FP-SVM.** Focused Probing using support vector machines with linear kernels [Joachims 1998] in conjunction with the same rule extraction technique used for FP-Bayes.

The query probes of these classifiers are typically short: The median query length is 1 word, average query length is 1.35 words, and maximum query length is 4 words. Further details about the characteristics of the classifiers are available in Gravano et al. [2003].

We also consider different values for the $\tau_{es}$ and $\tau_{ec}$ thresholds, which affect the granularity of sampling performed by the algorithm (see Section 3.1). All variations were tested with threshold $\tau_{es}$ ranging between 0 and 1. Low values of $\tau_{es}$ result in databases being pushed to more categories, which in turn results in larger document samples. To keep the number of experiments manageable, we fix the coverage threshold to $\tau_{ec} = 10$, varying only the specificity threshold $\tau_{es}$.

5.2.2 Shrinking and Frequency Estimation. Our experiments also evaluate the usefulness of our shrinkage (Section 4.2) and frequency estimation (Section 3.2) techniques. To evaluate the effect of shrinkage on content summary quality, we create the shrunk content summary $\tilde{R}(D)$ for each database $D$ and contrast its quality against that of the unshrunk content summary $\hat{S}(D)$. Similarly, to evaluate the effect of our frequency estimation technique on content summary quality, we consider the QBS and FPS summaries, both with and without this frequency estimation. We report results on the quality of content summaries before and after the application of our shrinkage algorithm.

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23Note that this slightly favors QBS in the experiments over the Controlled databases: The initial dictionary contains a superset of words that appear in each database in the Controlled dataset. Experiments that use the Web, TREC4, and TREC6 datasets are not affected by this bias.
To apply shrinkage, we need to classify each database into the 72-node topic hierarchy. Unfortunately, such classification is not available for TREC data, so for the TREC4 and TREC6 datasets we resort to our classification technique from Gravano et al. [2003], which we reviewed briefly in Section 2.3.24 A manual inspection of the classification results confirmed that they are generally accurate. For example, the TREC4 database all-83, with articles about AIDS, was correctly classified under the “Root→Health→Diseases→AIDS” category. Interestingly, in the case in which databases were not classified correctly, similar databases were still classified into the same (incorrect) category. For example, all-14, all-21, and all-44 are about middle-eastern politics and were classified under the “Root→Science→Social Sciences→History” category.

Unlike TREC4 and TREC6, for which no “external” classification of the databases is available, for the Web databases we do not have to rely on query probing for classification; instead we can use the categories assigned to databases in the Google Directory. For QBS, the classification of each database in our dataset was indeed derived from the Google Directory. For FPS, we can either use the (correct) Google Directory database classification, as for QBS, or rely on the automatically computed database classification that this technique derives during document sampling. We tried both choices and found only small differences in the experimental results. Therefore, for conciseness, we only report the FPS results for the automatically derived database classification. Finally, for the Controlled dataset, we use the automatically derived classification with $\tau_{es} = 0.25$ and $\tau_{ec} = 10$.

5.3 Database Selection Algorithms

The algorithms presented in this article (Sections 4.1 and 4.2.3) are built on top of underlying “base” database selection algorithms. We consider three well-known such algorithms from the literature.

—bGLOSS, as described in Gravano et al. [1999]. Databases are ranked for a query $q$ by decreasing score $s(q, D) = |D| \cdot \prod_{w \in q} \hat{p}(w|D)$.

—CORI, as described in French et al. [1999]. Databases are ranked for a query $q$ by decreasing score $s(q, D) = \sum_{w \in q} \frac{0.4 + 0.6 T I}{\hat{p}(w|D) \cdot |D| + 50 + 150 \cdot \frac{cw(D)}{mcw}}$, $I = \log\left(\frac{m + 0.5}{cf(w)}\right) / \log(m + 1.0)$, $cw(w)$ is the number of databases containing $w$, $m$ is the number of databases being ranked, $cw(D)$ is the number of words in $D$, and $mcw$ is the mean $cw$ among the databases being ranked. One potential problem with the use of CORI in conjunction with shrinkage is that virtually every word has $cf(w)$ equal to the number of databases in the dataset: Every word appears with nonzero probability in every shrunk content summary. Therefore, when we calculate $cw(w)$ for a word $w$ in our CORI experiments, we consider $w$ as present in a database $D$ only when $\text{round}(\hat{p}(w|D) \cdot \hat{p}(w|D)) \geq 1$.

—Language Modeling (LM), as described in Si et al. [2002]. Databases are ranked for a query $q$ by decreasing score $s(q, D) = \prod_{w \in q} (\lambda \cdot \hat{p}(w|D) + (1 - \lambda))$.

---

24We adapted the technique slightly so that each database is classified under exactly one category.
The LM algorithm is equivalent to the KL-based database selection method described in Xu and Croft [1999]. For LM, \( p(w|D) \) is defined differently than in Definition 2.1. Specifically, \( p(w|D) = \frac{tf(w,D)}{\sum_i tf(w_i,D)} \), where \( tf(w,D) \) is the total number of occurrences of \( w \) in \( D \). The algorithms described in Section 4.2 can be easily adapted to reflect this difference, by substituting this definition of \( p(w|D) \) for that in Definition 2.1. LM smooths the \( \hat{p}(w|D) \) probability with the probability \( \hat{p}(w|G) \) for a “global” category \( G \). In our experiments, we derive the probabilities \( \hat{p}(w|G) \) from the “Root” category summary and we use \( \lambda = 0.5 \), as suggested in Si et al. [2002].

We experimentally evaluate the aforesaid three database selection algorithms with three variations:

—**Plain.** Using unshrunk (incomplete) database content summaries extracted via QBS or FPS.

—**Shrinkage.** Using shrinkage when appropriate (as discussed in Section 4.2.3), again over database content summaries extracted via QBS or FPS.

—**Hierarchical.** Using unshrunk database content summaries (extracted via QBS or FPS) in conjunction with the hierarchical database selection algorithm from Section 4.1.

Finally, to evaluate the effect of our frequency estimation technique (Section 3.2) on database selection accuracy, we consider the QBS and FPS summaries both with and without this frequency estimation. Also, since stemming can help alleviate the data sparseness problem, we consider content summaries both with and without stemming.

### 6. EXPERIMENTAL RESULTS FOR CONTENT SUMMARY QUALITY

In this section, we evaluate alternative content summary construction techniques. We first focus on the impact of the choice of sampling algorithm on content summary quality in Section 6.1. Then, in Section 6.2 we show that databases classified under similar categories tend to have similar content summaries. Finally, in Section 6.3 we show that shrinkage-based content summaries are of higher quality than their unshrunk counterparts.

#### 6.1 Effect of Sampling Algorithm

Consider a database \( D \) and a content summary \( A(D) \) computed using an arbitrary sampling technique. We now evaluate the quality of \( A(D) \) in terms of how well it approximates the “perfect” content summary \( S(D) \), determined by examining every document in \( D \). In the following definitions, \( W_A \) is the set of words that appear in \( A(D) \), while \( W_S \) is the (complete) set of words that appear in \( S(D) \). Our experiments are over the Controlled dataset.

**Recall.** An important property of content summaries is their coverage of the actual database vocabulary. The weighted recall (wr) of \( A(D) \) with respect to \( S(D) \) is defined as

\[
wr = \frac{\sum_{w \in W_A \cap W_S} df(w)}{\sum_{w \in W_S} df(w)},
\]

which corresponds to the ctf ratio in Callan and Connell [2001]. This metric gives higher weight to more frequent words, but is calculated after stopwords (e.g., “a”, “the”) are removed,

so this ratio is not artificially inflated by the discovery of common words. We report the weighted recall for the different content summary construction algorithms in Figure 11(a). Variants of the Focused Probing technique achieve substantially higher \( wr \) values than do QBS-Ord and QBS-Lrd. Early during probing, Focused Probing retrieves documents covering different topics, and then sends queries of increasing specificity, retrieving documents with more specialized words. As expected, the coverage of Focused Probing summaries increases for lower values of the specificity threshold \( \tau_{es} \), since the number of
documents retrieved for lower thresholds is larger (e.g., 493 documents for FP-SVM with $\tau_{es} = 0.25$ versus 300 documents for QBS-Lrd): A sample of larger size, everything else being the same, is better for content summary construction. In general, the difference in weighted recall between QBS-Lrd and QBS-Ord is small, but QBS-Lrd has slightly lower $wr$ values due to the bias induced from querying only using previously discovered words. To understand whether low-frequency words are present in the approximate summaries, we resort to
the unweighted recall (ur) metric, defined as $ur = \frac{|WA \cap WS|}{|WS|}$. The $ur$ metric is the fraction of words in a database that are present in a content summary. Figure 11(b) shows trends similar to those for weighted recall, but the numbers are smaller, showing that lower-frequency words are not well represented in the approximate summaries.

Correlation of word rankings. The recall metric can be helpful to compare the quality of different content summaries. However, this metric alone is not enough, since it does not capture the relative ranks of words in the content summary by their observed frequency. To measure how well a content summary orders words by frequency with respect to the actual word frequency order in the database, we use the Spearman rank correlation coefficient (SRCC for short), which is also used in [Callan and Connell 2001] to evaluate the quality of the content summaries. (We use the version of SRCC that accounts for ties, as suggested by Callan and Connell [2001].) When two rankings are identical, then $SRCC = 1$; when they are uncorrelated, $SRCC = 0$; and when they are in reverse order, $SRCC = -1$. The results for the different algorithms are shown in Figure 11(c). Again, the content summaries produced by Focused Probing techniques have higher SRCC values than those for QBS-Lrd and QBS-Ord, hinting that Focused Probing retrieves a more representative sample of documents from the database.

Accuracy of frequency estimations. In Section 3.2, we introduced a technique to estimate the actual absolute frequencies of words in a database. To evaluate the accuracy of our predictions, we computed the average relative error $|df(w) - \hat{df}(w)|/df(w)$ for every word $w$ with actual frequency $df(w) > 3$ (including the large tail of less-frequent words would highly distort the relative-error.
classification, even for small estimation errors). Figure 11(d) reports the average relative-error estimates for our algorithms. We also applied our absolute frequency estimation algorithm of Section 3.2 to QBS-Ord and QBS-Lrd, even though this estimation is not part of the original algorithms in Callan and Connell [2001]. As a general conclusion, our technique provides a good ballpark estimate of the absolute frequency of the words.

**Efficiency.** To measure the efficiency of the probing methods, we report the sum of the number of queries sent to a database and the number of documents retrieved (“number of interactions”) in Figure 11(e); see Gravano et al. [2003] for a justification of this metric. Focused Probing techniques retrieve, on average, one document per query, while QBS-Lrd retrieves about one document for every two queries.25 QBS-Ord unnecessarily issues many queries that produce no document matches. The efficiency of the other techniques is correlated with their effectiveness. More expensive techniques tend to give better results. The exception is FP-SVM, which for \( \tau_{es} > 0 \) has the lowest cost (or cost close to the lowest one) and gives results of comparable quality with respect to the more expensive methods. As discussed earlier, the Focused Probing probes were generally short, with a maximum of four words and a median of one word per query.

**Recall, rank correlation, and efficiency for identical sample size.** We have seen that Focused Probing algorithms achieve better \( wr \) and SRCC values than do the QBS-Lrd and QBS-Ord algorithms. However, the Focused Probing algorithms generally retrieve a (moderately) larger number of documents than do QBS-Ord and QBS-Lrd, and the number of documents retrieved depends on how deeply into the categorization scheme the databases are classified. To test whether the improved performance of Focused Probing is just a result of larger sample size, we increased the sample size for QBS-Lrd to retrieve the same number of documents as each Focused Probing variant.26 We refer to the versions of QBS-Lrd that retrieve the same number of documents as FP-Bayes, FP-C4.5, FP-RIPPER, and FP-SVM as QBS-Bayes, QBS-C4.5, QBS-RIPPER, and QBS-SVM, respectively.

The \( wr \), \( ur \), and SRCC values for the alternative versions of QBS-Lrd are shown in Figures 12(a), 12(b), and 12(c), respectively. We observe that the \( wr \), \( ur \), and SRCC values of the QBS methods improve with a larger document sample, but are still lower than their Focused Probing counterparts; the difference is statistically significant at the 1% level according to a paired \( t \)-test. In general, the results show that Focused Probing methods are more effective than their QBS counterparts: The Focused Probing queries are generated by document classifiers and tend to “cover” distinct parts of the document space. In contrast, QBS methods query the database with words that appear in the retrieved documents, and these documents tend to contain words already present in the

25The average is computed over databases in the Controlled dataset, after the different content summary construction algorithms run to completion.

26We pick QBS-Lrd over QBS-Ord because the latter requires a much larger number of queries to extract its document sample: Most of its queries return no results (see Figure 11(e)), making it the most expensive method.
Fig. 12(a). Weighted recall as a function of the specificity threshold $t_{es}$, for the Controlled dataset and for the case where the FP and QBS methods retrieve the same number of documents; (b) unweighted recall as a function of the specificity threshold $t_{es}$, for the Controlled dataset and for the case where the FP and QBS methods retrieve the same number of documents.

sample. This difference is more pronounced in earlier stages of sampling, where Focused Probing sends more general queries. When Focused Probing starts sending queries for lower levels of the classification hierarchy, both Focused Probing and QBS demonstrate similar rates of vocabulary growth. The exact
point where the two techniques start performing similarly depends on the size of the database. For large databases, Focused Probing dominates QBS even at deep levels of the hierarchy, while for smaller databases the benefits of Focused Probing are only visible during the first and second levels of sampling.

Finally, we measured the number of interactions performed by the Focused Probing and QBS methods when they retrieve the same number of documents. The sum of the number of queries sent to a database and the number of documents retrieved (“number of interactions”) is shown in Figure 12(d). The average number of queries sent to each database is larger for the QBS methods than for their Focused Probing counterparts when they retrieve the same number of documents: QBS queries are derived from the already acquired vocabulary, and many of these words appear only in one or two documents, so a large fraction of the QBS queries return only documents that have been retrieved before. These queries increase the number of interactions for QBS, but do not retrieve any new documents.

For completeness, we ran the same set of experiments for the Web, TREC4, and TREC6 datasets. We use content summaries extracted from FP-SVM with specificity threshold $\tau_{es} = 0.25$ and coverage threshold $\tau_{ec} = 10$: We note that FP-SVM exhibits the best accuracy-efficiency tradeoff, while $\tau_{es} = 0.25$ leads to good database classification decisions as well (see Gravano et al. [2003]). We also use the respective QBS-SVM version of QBS. The results that we obtained (Table IV) were in general similar to those for the Controlled dataset. The main difference with the results obtained for the Controlled dataset is that the number of interactions is substantially lower for FP-SVM (and hence for
Fig. 12(d). Number of interactions per database as a function of the specificity threshold $\tau_{es}$, for the Controlled dataset and for the case where the FP and QBS methods retrieve the same number of documents.

Table IV. Weighted Recall, Unweighted Recall, Spearman Rank Correlation Coefficient, and Number of Interactions per Database

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Method</th>
<th>Metric</th>
<th>Interactions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Web</td>
<td>FP-SVM</td>
<td>0.887</td>
<td>0.520</td>
</tr>
<tr>
<td>Web</td>
<td>QBS-SVM</td>
<td>0.879</td>
<td>0.456</td>
</tr>
<tr>
<td>TREC4</td>
<td>FP-SVM</td>
<td>0.972</td>
<td>0.599</td>
</tr>
<tr>
<td>TREC4</td>
<td>QBS-SVM</td>
<td>0.943</td>
<td>0.428</td>
</tr>
<tr>
<td>TREC6</td>
<td>FP-SVM</td>
<td>0.975</td>
<td>0.662</td>
</tr>
<tr>
<td>TREC6</td>
<td>QBS-SVM</td>
<td>0.952</td>
<td>0.545</td>
</tr>
</tbody>
</table>

These results are for the Web, TREC4, and TREC6 datasets and for the case where FP-SVM and QBS-SVM retrieve the same number of documents.

QBS-SVM: Databases in the Controlled dataset are typically classified under multiple categories; in contrast, the databases in Web, TREC4, and TREC6 are generally classified under only one or two categories, and hence require much fewer queries for content summary construction than do Controlled databases.

Evaluation conclusions. Overall, Focused Probing techniques produce summaries of better quality than do QBS-Ord and QBS-Lrd, both in terms of vocabulary coverage and word-ranking preservation. The cost of Focused Probing in terms of number of interactions with the databases is comparable to that for QBS-Lrd (for $\tau_{es} > 0$), and significantly lower than that for QBS-Ord. Finally, the absolute frequency estimation technique of Section 3.2 gives good ballpark approximations of the actual frequencies.
6.2 Relationship Between Content Summaries and Categories

A key conjecture behind our database selection algorithms is that databases under the same category tend to have closely related content summaries. Thus, we can use the content summary of a database to complement the (incomplete) content summary of another database in the same category (Section 4.2). We now explore this conjecture experimentally using the Controlled, Web, TREC4, and TREC6 datasets.

Each database in the Controlled set is classified using \( \tau_s = 0.25 \) and \( \tau_c = 10 \), and following definition in Gravano et al. [2003]. By construction, we know the contents of all databases in the Controlled set, as well as their correct classification. For the Web dataset, we use the database classification as given by Open Directory. Finally, we classify the databases in the TREC4 and TREC6 datasets using the classification algorithm from Gravano et al. [2003], with \( \tau_{es} = 0.25 \) and \( \tau_{ec} = 10 \). Then, for each pair of databases \( D_i \) and \( D_j \) we measure

| — the number of categories that they share, numCategories, where |
| \[ \text{numCategories} = | \text{Path(Ideal}(D_i)) \cap \text{Path(Ideal}(D_j)) |, \] |
| and where Ideal(D) is the correct classification of D, Path(Ideal(D)) = \{ category c | c \in Ideal(D), or where c is an ancestor of some n \in Ideal(D) \}, for \( \tau_{es} = 0.25 \) and \( \tau_{ec} = 10 \); |
| — the wr, ur, and SRCC values of their correct content summaries. |

Figures 13(a), 13(b), and 13(c) report the wr, ur, and SRCC metrics, respectively, over all pairs of databases in the Controlled set and discriminated by numCategories. The larger the number of common categories between a pair of databases, the more similar their corresponding content summaries tend to be, according to the wr, ur, and SRCC metrics. Tables V(a), V(b), and V(c) report the wr, ur, and SRCC metrics, respectively, over all pairs of databases in the Web, TREC4, and TREC6 datasets, confirming the idea that databases
6.3 Effect of Shrinkage

We now report experimental results on the quality of the content summaries generated by the shrinkage technique from Section 4.2. To keep our experiments manageable, we use content summaries extracted from FP-SVM with specificity threshold $\tau_{sp} = 0.25$ and coverage threshold $\tau_{cov} = 10$, which give good classification decisions. We also pick QBS-Lrd over QBS-Ord, since the former method demonstrates similar performance at substantially smaller cost than the latter. (See Section 6.1 for a justification of this choice.) For conciseness, we classified under similar categories have more similar content summaries than those under different topics.
now refer to FP-SVM as FPS and to QBS-Lrd as QBS. We evaluate the content summaries using the Controlled, Web, TREC4, and TREC6 datasets.

Recall. We used the weighted and unweighted recall metrics to measure vocabulary coverage of shrunk content summaries. The shrunk content summaries include (with nonzero probability) every word in any content summary. Most words in any given content summary, however, tend to exhibit a very low probability. Therefore, not to inflate artificially the recall results (and conversely, not to hurt artificially the precision results), we drop from the shrunk content summaries every word $w$ with $\text{round}(|D| \cdot \hat{p}_D(w|D)) < 1$ during evaluation. Intuitively, we drop from the content summary all words that are estimated to appear in less than one document.

Table VI shows the weighted recall for different content summary construction techniques. Most methods exhibit high weighted recall, which shows that document sampling techniques identify the most frequent words in the database. Not surprisingly, shrinkage increases the (already high) $wr$ values and all shrinkage-based methods have close-to-perfect $wr$. This improvement is statistically significant in all cases: A paired $t$-test [Marques De Sá 2003] showed significance at the 0.01% level. The improvement for the Web set is higher compared to that for the TREC4 and TREC6 datasets: The Web set contains

<table>
<thead>
<tr>
<th>Dataset</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Web</td>
<td>0.83</td>
<td>0.89</td>
<td>0.90</td>
<td>0.91</td>
</tr>
<tr>
<td>TREC4</td>
<td>0.85</td>
<td>0.89</td>
<td>0.92</td>
<td>0.95</td>
</tr>
<tr>
<td>TREC6</td>
<td>0.86</td>
<td>0.88</td>
<td>0.89</td>
<td>0.92</td>
</tr>
</tbody>
</table>

The measure is for pairs of database content summaries as a function of the number of common categories in the database pairs and for the Web, TREC4, and TREC6 datasets.
larger databases, and the approximate content summaries are less complete than the respective approximate content summaries of TREC4 and TREC6. Our shrinkage technique becomes increasingly useful for larger databases. To understand whether low-frequency words are present in the approximate and shrunk content summaries, we use the unweighted recall metric. Table VI(b) shows that the shrunk content summaries have higher unweighted recall as well.

Finally, recall is higher when shrinkage is used in conjunction with the frequency estimation technique. This behavior is to be expected: When frequency estimation is enabled, the words introduced by shrinkage are close to their real frequencies, and are used in precision and recall calculations. When frequency

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Sampl. Method</th>
<th>Freq. Est.</th>
<th>Shrinkage</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Controlled</td>
<td>QBS</td>
<td>No</td>
<td>0.903</td>
</tr>
<tr>
<td></td>
<td>QBS</td>
<td>Yes</td>
<td>0.917</td>
</tr>
<tr>
<td></td>
<td>FPS</td>
<td>No</td>
<td>0.912</td>
</tr>
<tr>
<td></td>
<td>FPS</td>
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estimation is not used, the estimated frequencies of the same words are often below 0.5, and therefore not used in precision and recall calculations.

Precision. A database content summary constructed using a document sample contains only words that appear in the database. In contrast, the shrunk content summaries may include words not in the corresponding databases. To measure the extent to which “spurious” words are added (with high weight) by shrinkage in the content summary, we use the weighted precision \( wp \) of \( A(D) \) with respect to \( S(D) \), \( wp = \frac{\sum_{w \in W_A \cap W_S} df(w)}{\sum_{w \in W_A} df(w)} \). Table VII(a) shows that shrinkage decreases weighted precision by just 0.8% to 6%.

We also report the unweighted precision \( up \) metric, defined as \( up = \frac{|W_A \cap W_S|}{|W_A|} \). This metric reveals how many words introduced in a content summary do not
Table VIII. Spearman Correlation Coefficient

<table>
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<tr>
<th>Dataset</th>
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<th>Shrinkage</th>
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<td>0.628</td>
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appear in the complete content summary (or, equivalently, in the underlying database). Table VII(b) reports the results for the up metric, which show that shrinkage-based techniques have unweighted precision usually above 90% and always above 84%.

Word-ranking correlation. Table VIII shows that SRCC is higher for the shrunk content summaries. In general, SRCC is better for shrunk than for unshrunk content summaries (p < 0.001, according to a paired t-test): Not only do the shrunk content summaries have better vocabulary coverage (as the recall figures show), but also the newly added words tend to be ranked properly.

Word-frequency accuracy. Our shrinkage-based algorithm modifies the probability estimates \( p(w|D) \) in the approximate summaries \( A(D) \), in order to generate a summary whose probability distribution is closer to that of the original \( S(D) \). The KL-divergence compares the similarity of the \( A(D) \) estimates against the real values in \( S(D) \): \( KL = \sum_{w \in W_A \cap W_S} p(w|D) \cdot \log \frac{p(w|D)}{p(w|D)} \), where \( p(w|D) \) is defined as \( p(w|D) = \frac{tf(w,D)}{\sum_{i} tf(w_i,D)} \) and \( tf(w,D) \) is the total number of occurrences of \( w \) in \( D \). The KL metric takes values from 0 to infinity, with 0 indicating that the two content summaries being compared are equal.

Table IX shows that shrinkage helps decrease large KL values. (Recall that lower KL values indicate higher-quality summaries.) This is a characteristic of shrinkage [Hastie et al. 2001]: All summaries are shrunk towards some “common” content summary that has an average distance from all the summaries. This effectively reduces the variance of the estimations and leads to reduced estimation risk. However, shrinkage (moderately) hurts content-summary accuracy in terms of the KL metric in cases where KL is already low for the unshrunk summaries. We use this observation in our shrinkage-based database selection algorithm in Section 4.2.3, where our algorithm attempts to identify those cases where shrinkage is likely to help general database selection accuracy and avoids applying shrinkage in other cases.

Table IX. KL-Divergence

<table>
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<th>Dataset</th>
<th>Sampl. Method</th>
<th>Freq. Est.</th>
<th>Shrinkage Est.</th>
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*Evaluation conclusions.* The general conclusion from our experiments on content summary quality is that shrinkage drastically improves content summary recall at the expense of precision. The high weighted precision of shrinkage-based summaries suggests that the spurious words introduced by shrinkage appear with low weight in the summaries, which should reduce any potential negative impact on database selection. Next, we present experimental evidence that the loss in precision ultimately does not hurt, since shrinkage improves overall database selection accuracy.

### 7. EXPERIMENTAL RESULTS FOR DATABASE SELECTION ACCURACY

In this section, we evaluate the accuracy of the database selection algorithms that we presented in this article. We first describe our evaluation metric, and then we study the performance of the proposed database selection algorithms under a variety of settings. Just as in Section 6.3, we use FP-SVM (for conciseness, FPS) with specificity threshold $\tau_{es} = 0.25$ and coverage threshold $\tau_{ec} = 10$, and QBS-Lrd (for conciseness, QBS) as underlying content summary construction algorithms.

Consider a ranking of the databases $\vec{D} = D_1, \ldots, D_m$ according to the scores produced by a database selection algorithm for some query $q$. To measure the “goodness” or general quality of such a rank, we follow an evaluation methodology that is prevalent in the information retrieval community, and consider the number of documents in each database that are relevant to $q$, as determined by a human judge [Salton and McGill 1983]. Intuitively, a good rank for a query includes (at the top) those databases with the largest number of relevant documents for the query. If $r(q, D_i)$ denotes the number of $D_i$ documents that are relevant to query $q$, then $A(q, \vec{D}, k) = \sum_{i=1}^{k} r(q, D_i)$ measures the total number of relevant documents among the top-$k$ databases in $\vec{D}$. To normalize this measure, we consider a hypothetical, “perfect” database rank $\vec{D}_H = D_{h_1}, \ldots, D_{h_m}$ in which databases are sorted by their $r(q, D_{h_i})$ value. (This
is, of course, unknown to the database selection algorithm.) Then, we define the $R_k$ metric for a query and database rank $D$ as $R_k = \frac{A(q, D, k)}{A(q, D_H, k)}$ [Gravano et al. 1999]. A “perfect” ordering of $k$ databases for a query yields $R_k = 1$, while a (poor) choice of $k$ databases with no relevant content results in $R_k = 0$. We note that when a database receives the default score from a database selection algorithm (i.e., when the score assigned to a database for a query is equal to that assigned to an empty query), we consider that the database is not selected for searching. This sometimes results in a database selection algorithm selecting fewer than $k$ databases for a query.

The $R_k$ metric relies on human-generated relevance judgments for the queries and documents. For our experiments on database selection accuracy, we focus on the TREC4 and TREC6 datasets, which include queries and associated relevance judgments. We use queries 201–250 from TREC-4 with the TREC4 dataset and queries 301–350 from TREC-6 with the TREC6 dataset. The TREC-4 queries are long, with 8–34 words and an average of 16.75 words per query. The TREC-6 queries are shorter, with 2–5 words and an average of 2.75 words per query.

We considered eliminating stopwords (e.g., “the”) from the queries, as well as applying stemming to the query and document words (e.g., so that a query [computers] matches documents with the word “computing”). While the results improve with stopword elimination, a paired $t$-test showed that the difference in performance is not statistically significant; therefore, we only report results with stopword elimination. Stemming tends to improve performance for small values of $k$; the results are mixed when $k > 10$.

Figures 14(a)–14(d) show results for the CORI database selection algorithm. We used both the TREC4 and TREC6 datasets and queries, as well as the QBS and FPS content summary construction strategies (Section 5.2). We consider applying CORI over “unshrunk” content summaries (QBS-Plain and FPS-Plain), using the adaptive shrinkage-based strategy (QBS-Shrinkage and FPS-Shrinkage), and using the hierarchical algorithm (QBS-Hierarchical and FPS-Hierarchical). Figures 15(a)–15(d) show the results for the bGlOSS database selection algorithm, while Figures 16(a)–16(d) show the results for the LM database selection algorithm.

Overall, a paired $t$-test shows that QBS-Shrinkage improves the database selection performance over QBS-Plain, and this improvement is statistically significant ($p < 0.05$). Moreover, FPS-Shrinkage improves the database selection performance relative to FPS-Plain, but this improvement is statistically significant only when $k < 10$. We now describe the details of our findings.

Shrinkage versus plain. The first conclusion from our experiments is that QBS-Shrinkage and FPS-Shrinkage improve performance compared to
Fig. 14(a). The $R_k$ ratio for CORI with stemming over the TREC4 dataset.

Fig. 14(b). The $R_k$ ratio for CORI without stemming over the TREC4 dataset.

Fig. 14(c). The $R_k$ ratio for CORI with stemming over the TREC6 dataset.

Fig. 14(d). The $R_k$ ratio for CORI without stemming over the TREC6 dataset.

Fig. 15(a). The $R_k$ ratio for bGlOSS with stemming over the TREC4 dataset.

Fig. 15(b). The $R_k$ ratio for bGlOSS without stemming over the TREC4 dataset.

Fig. 15(c). The $R_k$ ratio for bGlOSS with stemming over the TREC6 dataset.

Fig. 15(d). The $R_k$ ratio for bGlOSS without stemming over the TREC6 dataset.
Fig. 16(a). The $R_k$ ratio for LM with stemming over the TREC4 dataset.

Fig. 16(b). The $R_k$ ratio for LM without stemming over the TREC4 dataset.

Fig. 16(c). The $R_k$ ratio for LM with stemming over the TREC6 dataset.

Fig. 16(d). The $R_k$ ratio for LM without stemming over the TREC6 dataset.

QBS-Plain and FPS-Plain, respectively. Shrinkage helps because new words are added in the content summaries in a database- and category-specific manner. In Table X, we report the number of times shrinkage was applied for each database-query pair and for each database selection algorithm. Since the queries for TREC6 are shorter, shrinkage was applied comparatively fewer times for TREC6 than for TREC4. Also, shrinkage was applied more frequently for bGlOSS than for LM and CORI. Specifically, bGlOSS does not have any form of smoothing and assigns zero scores to databases whose content summaries do not contain a query word. This results in high variance for the bGlOSS scores, which in turn triggers the application of shrinkage.

Interestingly, Table X shows that shrinkage is applied relatively few times overall, yet its impact on database selection accuracy is large, as we have seen. To understand why, note that the Table X figures refer to database-query pairs. We have observed that the application of shrinkage to even a few critical databases for a given query can sometimes dramatically improve the quality of the database rank that is produced for the query. As a real example of this phenomenon, consider the TREC-6 query [unexplained highway accidents] and database all-2, which contains 92.5% of all relevant documents for the query. Using the LM algorithm (for both FPS and QBS), database all-2 is ranked 16th, resulting in low $R_k$ values for any $k < 16$. Our adaptive shrinkage algorithm decides to use shrinkage for this specific database-query pair, and database all-2 is ranked 3rd after application of shrinkage. This results in substantially larger $R_k$ values for the shrinkage-based algorithms for $3 \leq k \leq 15$. While our adaptive database selection algorithm applied shrinkage to just 5% of the databases for this query (i.e., for just 5 databases out of 100), the resulting database rank for the query is significantly better than the rank produced with no shrinkage. In general, even limited applications of shrinkage tend to have significant effect on the $R_k$ ranking: The distribution of relevant documents across databases is typically skewed, and only a small number of databases contain the majority of relevant documents. Therefore, by ranking the important databases accurately, we can substantially improve the database selection performance.

**Shrinkage versus hierarchical.** QBS-Hierarchical and FPS-Hierarchical generally outperform their “plain” counterparts. This confirms our observation that categorization information helps compensate for incomplete summaries. Exploiting this categorization via shrinkage results in even higher accuracy:

This effect is not only limited to TREC datasets, but is true for the web at large.

QBS-Shrinkage and FPS-Shrinkage significantly outperform QBS-Hierarchical and FPS-Hierarchical. This improvement is due to the flat nature of our shrinkage method: While QBS-Shrinkage and FPS-Shrinkage can rank the databases globally, QBS-Hierarchical and FPS-Hierarchical have to make irreversible choices at each category level of the hierarchy. Even when a chosen category contains only a small number of databases with relevant documents, the hierarchical algorithm continues to select (irrelevant) databases from the (relevant) category. When a query cuts across multiple categories, the hierarchical algorithm might fail to select the appropriate databases. In contrast, our shrinkage-based approach can potentially select databases from multiple categories and hence manages to identify the appropriate databases for a query, regardless of whether they are similarly classified or not.

Adaptive versus universal application of shrinkage. The strategy in Section 4.2.3 dynamically decides when to apply shrinkage for database selection. To understand whether this decision step is necessary, we evaluated the performance of the algorithms when we always decide to use shrinkage (i.e., when the $\hat{R}(D_i)$ content summary is always chosen in Figure 10). Figures 17(a)–(b) and 18(a)–(b) show the TREC4 results for CORI and bGLOSS, with QBS-Universal and FPS-Universal denoting universal application of shrinkage.29 The only case where QBS-Universal and FPS-Universal are better than QBS-Plain and FPS-Plain, respectively, is for bGLOSS (Figures 18(a) and (b)): Unlike CORI and LM, bGLOSS does not have any form of smoothing already built-in, so if a query word is not present in a content summary, bGLOSS assigns a zero score to the database. Unlike bGLOSS, CORI and LM perform worse when we apply shrinkage universally than when we do so adaptively. The only exception is for content summaries created without the use of stemming and only for small values of $k$, but even in this case the small improvement is not statistically significant. This result indicates that CORI and LM handle incomplete content summaries in a more graceful way than does bGLOSS, since both CORI and LM have a form of smoothing already embedded.

Frequency estimation. We also examined the effect of frequency estimation (Section 3.2) on database selection. Figures 19(a)–(d) show the results for CORI over TREC4 and TREC6. In general, frequency estimation affected only the performance of the CORI database selection algorithm, and had only a small effect on the performance of bGLOSS and LM, so we do not show plots for these two techniques. The reason is that bGLOSS and LM rely on probabilities that remain virtually unaffected after the frequency estimation step. In contrast, CORI relies on document frequencies. Figures 19(a)–(d) show that when shrinkage is used, frequency estimation improves the performance of CORI, by 10%–30% for small values of $k$, with respect to the case where raw word-frequencies for the document sample are used. Interestingly, frequency estimation alone, that is, without shrinkage, does not improve database selection as much, hinting that more accurate frequency estimates only improve database selection accuracy substantially when the underlying content summaries are sufficiently complete.

29The results for TREC6 are similar, while the results for LM are analogous to those for CORI.
Evaluation conclusions. A general conclusion from the experiments is that the *adaptive* application of shrinkage significantly improves database selection when selection decisions are based on sparse content summaries. An interesting observation is that the universal application of shrinkage is not always beneficial, indicating that for cases where selection decisions are already accurate, shrinkage negatively affects the selection process. Another conclusion is that stemming-based summaries are typically better than their nonstemmed counterparts, since stemming reduces data sparseness. The difference is significant for small numbers of selected databases, which indicates that stemming results in better database rankings.

8. RELATED WORK

This section addresses literature relevant to the topics covered in this article. Portions of this article appeared in Ipeirotis and Gravano [2002, 2004]. First, Section 8.1 reviews work on database selection. Then, Section 8.2 discusses related work for content summary construction. Finally, Section 8.3 summarizes various applications of query probing, a technique that we used extensively in this article.

8.1 Database Selection

A large body of work has been devoted to distributed information retrieval, or metasearching, over text databases. As we discussed, a crucial task for a
metasearcher is database selection, which requires that the metasearcher have summaries of the database contents.

Early database selection techniques relied on human-generated database descriptions. WAIS [Kahle et al. 1993] uses such descriptions and ranks databases according to their similarity to the queries. In Search Broker [Manber and Bigot 1997], each database is manually tagged with two or three category index descriptors. At query time, users specify the query category and then Search Broker selects the appropriate databases. Chakravarthy and Haase, Jr. [1995] use Wordnet [Fellbaum 1998] to complement manually assigned keywords that are used to describe each database for database selection.

More robust database selection approaches rely on statistical metadata about the contents of the databases, generally following the type of content summary used in this article. CORI [Callan et al. 1995; Xu and Callan 1998] uses inference networks together with this kind of content summary to select the best databases for a query. (We used CORI for our experiments in Section 7.) GlOSS [Gravano et al. 1999] uses content summaries and selects databases for a query according to some notion of goodness for a query. GlOSS can choose among a variety of definitions of goodness, some of which depend on the retrieval model supported by the databases. (We used bGlOSS, a variant of GlOSS originally introduced for Boolean databases, for our experiments in Section 7.) Yuwono and Lee [1997] use content summaries and rank databases according
Fig. 19(a). The $R_k$ ratio for CORI with stemming over the TREC4 dataset, for summaries generated with (“-FreqEst”) and without (“-NoFreqEst”) the use of frequency estimation.

Fig. 19(b). The $R_k$ ratio for CORI without stemming over the TREC4 dataset, for summaries generated with (“-FreqEst”) and without (“-NoFreqEst”) the use of frequency estimation.

Fig. 19(c). The $R_k$ ratio for CORI with stemming over the TREC6 dataset, for summaries generated with (“-FreqEst”) and without (“-NoFreqEst”) the use of frequency estimation.

Fig. 19(d). The $R_k$ ratio for CORI without stemming over the TREC6 dataset, for summaries generated with (“-FreqEst”) and without (“-NoFreqEst”) the use of frequency estimation.
to the cue validity of the query words: A query word $w$ has high cue validity for a database $D$ if the probability of observing $w$ in $D$ is comparatively higher than in other databases. Meng et al. [1999, 1998] also rely on content summaries to identify databases that contain the highest number of documents similar to a query, and similarity is computed using the cosine similarity metric. Meng et al. use a variety of methods to estimate the weight of words in the database, and propose to keep significant covariance statistics for word pairs that appear often together. The storage requirements for the content summaries in Meng et al. [1998] are much higher compared to other methods that ignore the covariance statistics, such as Callan et al. [1995], Xu and Callan [1998], Gravano et al. [1999], and Yuwono and Lee [1997], which we described before. In a similar approach, Yu et al. [2001] rank databases for a query according to the highest similarity of any document in each database to the query. Baumgarten [1999, 1997] proposes a probabilistic framework for database selection and uses content summaries to derive the $\hat{p}(w|D)$ probability estimates that are used during querying. Most approaches that use content summaries rely either on access to all documents or on metadata directly exported by the databases, using, for example, a protocol like STARTS [Gravano et al. 1997].

French et al. [1999, 1998], Powell et al. [2000], and Powell and French [2003] present experimental evaluations of database selection algorithms. Their main conclusion is that CORI is robust and performs better than other database selection algorithms for a variety of datasets. Results by Xu and Croft [1999] and Si et al. [2002] indicate that a language modeling (LM) approach for database selection works better than CORI for topically focused databases. (We used the LM algorithm for our experiments in Section 7.) Xu and Croft [1999] and Larkey et al. [2000] show that organizing documents by topic helps improve database selection accuracy. Our results in Section 7 are consistent with these findings, since they show that classification-aware database selection algorithms perform better than algorithms that ignore classification information.

Our database selection techniques in Section 4 are built on top of an arbitrary “base” database selection algorithm. We reported experiments using CORI, hGLOSS, and LM. Our experimental results show that our techniques improve database selection—in the face of sparse data—when used in conjunction with a variety of existing flat algorithms. In the future, our techniques can continue to leverage new database selection algorithms that rely on content summaries to make the selection decisions. Another promising direction for future research is to extend our smoothing models for database selection algorithms that not only keep a content summary for each database but also exploit the actual documents retrieved during document sampling (e.g., Si and Callan [2005, 2004a, 2003], Hawking and Thomas [2005], and Shokouhi [2007]).

Other database selection algorithms rely on hierarchical classification schemes (mostly for “efficiency”) to direct queries to appropriate categories of the hierarchy [Dolin 1998; Sheldon 1995; Gravano et al. 1999; Choi and Yoo 2001; Yu et al. 1999]. The hierarchical database selection algorithm in Sheldon [1995] uses intentionally small content summaries that contain only the high-frequency terms that characterize each category. The hGLOSS
system [Gravano et al. 1999] focuses on the efficiency of selection and does not exploit any topic similarities of the databases. Similarly, the hierarchical organization in Dolin [1998] focuses on efficiency and does not exploit the clustering of similar databases under the same categories. Fuhr [1999] briefly discusses the hierarchical database selection problem, but no special clustering of similar databases is considered to improve the hierarchical selection task. The aforementioned hierarchical algorithms also need access to all documents or to metadata directly exported by the databases. Our hierarchical database selection algorithm in Section 4.1 first appeared in Ipeirotis and Gravano [2002]; this algorithm uses a topic hierarchy not only for efficiency, but also for improving the quality of database selection decisions in the presence of sparse content summaries.

Other approaches rely on users providing relevance judgments to create a profile of each database. Voorhees et al. [1995] use a set of training queries to learn the usefulness of each database and to decide how many documents to retrieve from each. ProFusion [Gauch et al. 1996] and SavvySearch [Dreilinger and Howe 1997] also exploit historic data to learn the performance of each database for various types of queries. Then, databases that exhibit higher performance for a query are preferred over others. Fuhr [1999] uses a decision-theoretic model to decide whether to use a database and to determine how many documents to retrieve from a selected database. The method in Fuhr [1999] tries to minimize the cost of retrieval and assumes that the precision-recall curves of the underlying retrieval system either are known or can be estimated.

8.2 Constructing Database Content Summaries

Unfortunately, hidden-web text databases do not usually export any metadata about their contents nor offer immediate access to them. Callan et al. [2001, 1999] probe databases with semi-random queries to extract content summaries from autonomous databases. (See Section 2 for a detailed discussion of this technique.) We used Callan et al.’s algorithm extensively in our experiments of Sections 6 and 7. Monroe et al. [2002] present and evaluate small variations of the algorithm from Callan et al. [1999] and Callan and Connell [2001]. Craswell et al. [2000] compared database selection algorithms in the presence of incomplete content summaries extracted using document sampling, and observed that algorithm performance deteriorates with respect to its behavior over complete summaries. Sugiura and Etzioni [2000] proposed the Q-Pilot technique, which uses query expansion to route web queries to the appropriate search engines. It also characterizes databases using words that appear in the webpages that host the search interfaces, as well as words that appear in other webpages that link to the databases. We used an adaptation of Q-Pilot for content summary generation in a preliminary experimental evaluation [Ipeirotis and Gravano 2002] of our hierarchical database selection algorithm of Section 4.1. Our experiments showed that the Q-Pilot content summaries are not sufficient for accurate database selection. Hawking and Thistlewaite [1999] used query probing to perform database selection by ranking databases by similarity to a
given query. Their algorithm assumed that the query interface to the database can handle normal queries and query probes differently, and that the cost to handle query probes is smaller than that for normal queries.

A preliminary version of the algorithm of Section 3 for constructing content summaries appeared in Ipeirotis and Gravano [2002]. The frequency estimation algorithm in Ipeirotis and Gravano [2002] managed to produce relatively accurate frequency estimates for database words that appear in sample-based content summaries. However, a problem with this algorithm is the assumption that the rank of a word in a database coincides with the word’s rank in a document sample extracted from the database. Unfortunately, this assumption does not hold in general, and is largely false for words that appear in a database only a relatively small number of times. In Section 3.2, we presented an improved frequency estimation algorithm that addresses this problem and produces significantly more accurate word-frequency estimates for database words that appear only a relatively small number of times.

Along a related research direction, Si and Callan [2003] show that database selection performance can be improved by considering database size estimates within their ReDDE database selection algorithm. ReDDE retains the documents retrieved during content summary construction and uses this document sample to estimate the distribution of relevant documents across databases. Further studies by Si and Callan [2004b] show that CORI and LM are only marginally affected when used in conjunction with the database size estimation method from Si and Callan [2003]. This result is consistent with the behavior that we observed for CORI (without use of shrinkage) with our frequency estimation method.

Our content summary construction technique in Section 4.2 appeared in Ipeirotis and Gravano [2004] and is based on the work by McCallum et al. [1998], who introduced a shrinkage-based approach for hierarchical document classification in the face of sparse data. Shrinkage is a form of smoothing, and smoothing has been used extensively in the area of speech recognition [Jelinek 1999] to improve probability estimates in language models. Language modeling has also been used for information retrieval [Croft and Lafferty 2003]. Notably, smoothing is present in recent language modeling approaches to information retrieval [Zhai and Lafferty 2004, 2002, 2001]. An interesting direction for future work is to examine the performance of smoothing models other than shrinkage-based for database selection, especially in the presence of database classification information.

Liu et al. [2004] estimate the potential inaccuracy of the database rank produced for a query by a database selection algorithm. If this inaccuracy is unacceptably large, then the query is dynamically evaluated on a few carefully chosen databases to reduce the uncertainty associated with the database rank. This work does not take content summary accuracy into consideration. In contrast, in Section 4.2.3, we addressed the scenario where summaries are derived from document samples (and are hence incomplete) and decide dynamically whether shrinkage should be applied, without actually querying databases during database selection. The bulk of Section 4.2.3 appeared originally in Ipeirotis and Gravano [2004], where we described a generic method for computing the mean

and variance of a database score distribution when using sample-based content summaries. The method in Ipeirotis and Gravano [2004] did not use the fact that most database selection algorithms assume independence of the query words. We will exploit this property in Appendix B to substantially improve both the accuracy and runtime performance of the mean-variance computation, which in turn improves substantially the runtime performance of our database selection algorithm of Section 4.2.3.

8.3 Miscellaneous Applications of Query Probing

In this article, we used query probing for the extraction of content summaries from text databases. Query probing has helped in other related tasks. Gravano et al. [2003] use a small number of query probes derived using machine learning techniques to categorize a text database in a topic hierarchy. (We briefly reviewed this algorithm in Section 2.3 and used it extensively in subsequent sections.) Perkowitz et al. [1997] use it to automatically understand query forms and to extract information from web databases to build a comparative shopping agent. New forms of crawlers [Raghavan and García-Molina 2001] use query probing to automatically interact with web forms and crawl the contents of hidden-web databases. Cohen and Singer [1996] use RIPPER to learn queries that mainly retrieve documents in a specific category. The queries are used at a later time to retrieve new documents in this category. Flake et al. [2002] extract rules from nonlinear SVMs that identify documents with a common characteristic (e.g., “calls for papers”). The generated rules are used to modify queries sent to a search engine, so that the queries retrieve mostly documents of the desired kind. Grefenstette and Nioche [2000] use query probing to determine the use of different languages on the web. The query probes are words that appear only in one language. The number of matches generated for each probe is subsequently used to estimate the number of webpages written in each language. Ghani et al. [2001] automatically generate queries to retrieve documents written in a specific language. Meng et al. [1999] used guided query probing to determine sources of heterogeneity in the algorithms used to index and search locally at each text database. Bergholz and Chidlovskii [2004] probe a database with a carefully selected set of queries to identify the characteristics of the query language. Finally, the QXtract system [Agichtein and Gravano 2003] automatically generates queries to improve the efficiency of a given information extraction system, such as Snowball [Agichtein and Gravano 2000] or Proteus [Yangarber and Grishman 1998], over large text databases. Specifically, QXtract learns queries that tend to match those database documents that are useful for the extraction task at hand. The information extraction system can then focus only on these documents, which results in large performance improvements.

9. CONCLUSION

Database selection is critical to building efficient metasearchers that interact with potentially large numbers of databases. Exhaustively searching all available databases to answer each query is impractical (or even not possible) in
increasingly common scenarios. Current database selection algorithms rely on statistical summaries about the contents of the databases, in order to select the best databases for a given query; unfortunately, databases accessible through the web do not generally export these statistics. In this article, we presented efficient algorithms for constructing content summaries for such databases. Our algorithms create content summaries of higher quality than alternative approaches, and additionally categorize databases in a classification scheme. We also presented a shrinkage-based technique that further improves the quality of the generated content summaries. Shrinkage-based content summaries are more complete than their unshrunk counterparts. Our shrinkage-based technique achieves this performance gain efficiently, without requiring any increase in size of the document samples.

We also presented techniques for improving the performance of database selection algorithms in the case where database content summaries are derived from relatively small document samples. Such summaries are typically incomplete, and this can hurt the performance of database selection algorithms. We showed that classification-aware database selection algorithms can significantly improve the accuracy of selection decisions in the face of incomplete content summaries. Both the hierarchical database selection algorithm of Section 4.1 and the adaptive, shrinkage-based algorithm of Section 4.2 perform better than their counterparts that do not exploit database classification. Furthermore, we showed that the shrinkage-based strategy outperforms the hierarchical database selection algorithm: The hierarchical algorithm initially selects databases under a single subtree of the classification hierarchy, thus failing to select appropriate databases for queries that cut across multiple categories. Shrinkage, on the other hand, embeds the category information in the content summaries. Therefore, a flat database selection algorithm can exploit the classification information without being constrained by the classification hierarchy.

APPENDIXES

A. ESTIMATING SCORE DISTRIBUTIONS

Section 4.2.3 discussed how to estimate the uncertainty associated with a database score for a query. Specifically, this estimate relies on the probability $P$ of the different possible query keyword frequencies. To compute $P$, we assume independence of the words in the sample, as

$$P = \prod_{k=1}^{n} p(d_k|s_k),$$

where $p(d_k|s_k)$ is the probability that $w_k$ occurs in $d_k$ documents in database $D$, given that it occurs in $s_k$ documents in sample $S$. Using the Bayes rule, we have

$$p(d_k|s_k) = \frac{p(s_k|d_k)p(d_k)}{\sum_{i=0}^{|D|} p(i)p(s_k|i)}.$$  

To compute $p(s_k|d_k)$, we assume that the presence of each word $w_k$ follows a binomial distribution over the $S$ documents, with $|S|$ trials and probability of
success \( \frac{d_k}{|D|} \) for every trial. Then,

\[
p(s_k|d_k) = \left( \frac{|S|}{s_k} \right) \left( \frac{d_k}{|D|} \right)^{s_k} \left( 1 - \frac{d_k}{|D|} \right)^{|S|-s_k},
\]

\[
p(d_k|s_k) = \frac{p(d_k)}{\sum_{i=0}^{|D|} \left( p(i) \left( \frac{i}{|D|} \right)^{s_k} \left( 1 - \frac{i}{|D|} \right)^{|S|-s_k} \right)}.
\]

Finally, to compute \( p(d_k) \) we use the well-known fact that the distribution of words in text databases tends to follow a power law [Mandelbrot 1988]: Approximately \( cf^\gamma \) words in a database have frequency \( f \), where \( c \) and \( \gamma \) are database-specific constants (\( c > 0, \gamma < 0 \)). Then,

\[
p(d_k) = \frac{cd_k^\gamma}{\sum_{i=1}^{|D|} ci^\gamma} = \frac{d_k^\gamma}{\sum_{i=1}^{|D|} i^\gamma}.
\]

Interestingly, \( \gamma = \frac{1}{B} - 1 \), where \( B \) is a parameter of the frequency-rank distribution of the database [Adamic 2002] and can be computed as described in Section 3.2.

### B. ESTIMATING SCORE VARIANCE

The adaptive algorithm in Figure 10 computes the mean and variance of the query-score distribution for a database to decide whether to use shrinkage for the database content summary. In Section 4.2.3, we outlined a method for computing the mean and variance relatively efficiently for any arbitrary database selection algorithm. This computation can be made even faster for the large class of database selection algorithms that assume independence of the query words. For example, bGIOSS, CORI, and LM, the database selection algorithms that we used in our experiments, belong to this class. For these algorithms, we can calculate the mean and variance of the subscore associated with each query word separately, and then combine these word-level mean and variance values to compute the final-score mean and variance for the query. We show the derivation of variance\(^{30} \) for bGIOSS and CORI. The computation of variance for LM is similar to the one for bGIOSS.\(^{31} \)

#### Estimating Score Variance for bGIOSS

bGIOSS defines the score \( s(q, D) \) of a database \( D \) for a query \( q \) as

\[
s(q, D) = |D| \cdot \prod_{w \in q} \hat{p}(w|D).
\]

---

\(^{30}\)Computation of the mean score is simpler and the derivation is analogous to the variance computation presented here.

\(^{31}\)In the computation of mean and variance for LM, we treat the values of \( \hat{p}(w|G) \) as constants, since the variance of the random variable \( \hat{p}(w|G) \) is negligible compared to that of \( \hat{p}(w|D) \).
By definition of variance, we have
\[
\text{Var}(s(q, D)) = E[s(q, D)^2] - (E[s(q, D)])^2
\]
\[
= E \left[ |D| \cdot \prod_{w \in q} p(w | D) \right]^2 - \left( E \left[ |D| \cdot \prod_{w \in q} p(w | D) \right] \right)^2
\]
\[
= |D|^2 \cdot E \left[ \prod_{w \in q} p(w | D) \right]^2 - |D|^2 \cdot \left( E \left[ \prod_{w \in q} p(w | D) \right] \right)^2.
\]
Since the \( p(w | D) \)'s are assumed to be independent, we have
\[
E \left[ \prod_{w \in q} p(w | D) \right]^2 = \prod_{w \in q} E \left[ p(w | D) \right]^2
\]
\[
\left( E \left[ \prod_{w \in q} p(w | D) \right] \right)^2 = \left( \prod_{w \in q} E \left[ p(w | D) \right] \right)^2.
\]
Therefore,
\[
\text{Var} (s(q, D)) = |D|^2 \cdot \left( \prod_{w \in q} E \left[ p(w | D) \right]^2 - \left( \prod_{w \in q} E \left[ p(w | D) \right] \right)^2 \right).
\]
The mean values of the distributions of \( p(w | D) \) and \( p(w | D)^2 \) can be computed using the results from Appendix A. Since \( p(w | D) \) depends only on the frequency \( s_w \) of the word \( w \) in \( \hat{S}(D) \), we have
\[
E \left[ p(w | D) \right] = \sum_{i=1}^{|D|} \frac{i}{|D|} p(i | s_w)
\]
\[
E \left[ p(w | D)^2 \right] = \sum_{i=1}^{|D|} \left( \frac{i}{|D|} \right)^2 p(i | s_w)
\]
We can see that the variance \( \text{Var} (s(q, D)) \) can be computed efficiently because there is no need to consider frequency combinations, unlike the case for a generic database selection algorithm (see Section 4.2.3).

Estimating Score Variance for CORI
CORI defines the score \( s(q, D) \) of a database \( D \) for a query \( q \) as
\[
s(q, D) = \sum_{w \in q} \frac{0.4 + 0.6 \cdot T_w \cdot I_w}{|q|} = 0.4 + 0.6 \sum_{w \in q} \frac{T_w \cdot I_w}{|q|}
\]
\[
T_w = \frac{p(w | D) \cdot |D|}{p(w | D) \cdot |D| + 50 + 150 \cdot \frac{cw(D)}{mcw}} \quad \text{and} \quad I_w = \log \left( \frac{m + 0.5}{cf(w)} \right) / \log (m + 1.0)
\]
where \( cf(w) \) is the number of databases containing \( w \), \( m \) is the number of databases being ranked, \( cw(D) \) is the number of words in \( D \), and \( mcw \) is the mean
among the databases being ranked. For simplicity in our following calculations, we assume that \( cf(w) \) and \( cw(D) \) are constants, since the variance of their values is small compared to other components of the CORI formula. In this case, \( I_w \) is also constant. Then, by definition of variance we have

\[
\text{Var}(s(q, D)) = E[(s(q, D))^2] - (E[s(q, D)])^2
\]

\[
= E \left[ \left( 0.4 + 0.6 \cdot \sum_{w \in q} \frac{T_w \cdot I_w}{|q|} \right)^2 \right] - \left( E \left[ 0.4 + 0.6 \cdot \sum_{w \in q} \frac{T_w \cdot I_w}{|q|} \right] \right)^2
\]

\[
= \frac{0.36}{|q|^2} \cdot \left( \sum_{w \in q} E \left[ T_w^2 \cdot I_w \right] \right) - \frac{0.36}{|q|^2} \cdot \left( \sum_{w \in q} E \left[ T_w \cdot I_w \right] \right) - \sum_{w, w_j \in q, i \neq j} E \left[ T_w \cdot I_w \right] \cdot E \left[ T_{w_j} \cdot I_{w_j} \right]
\]

By assuming independence of the words \( w \) in the query, the variables \( T_{w_i} \) and \( T_{w_j} \) are independent if \( i \neq j \), and we have

\[
\sum_{w, w_j \in q, i \neq j} E \left[ T_{w_i} \cdot I_{w_i} \cdot T_{w_j} \cdot I_{w_j} \right] = \sum_{w, w_j \in q, i \neq j} E \left[ T_{w_i} \cdot I_{w_i} \right] \cdot E \left[ T_{w_j} \cdot I_{w_j} \right]
\]

Therefore,

\[
\text{Var}(s(q, D)) = \frac{0.36}{|q|^2} \left( \sum_{w \in q} I_w^2 \cdot (E[T_w^2] - (E[T_w])^2) \right)
\]

Again, the distribution of the random variables \( T_w \) and \( T_w^2 \) can be computed using the results from Appendix A. The mean values of the distributions can be computed efficiently, since there is no need to consider frequency combinations, unlike the case for a generic database selection algorithm (see Section 4.2.3).

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Classification-Aware Hidden-Web Text Database Selection


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